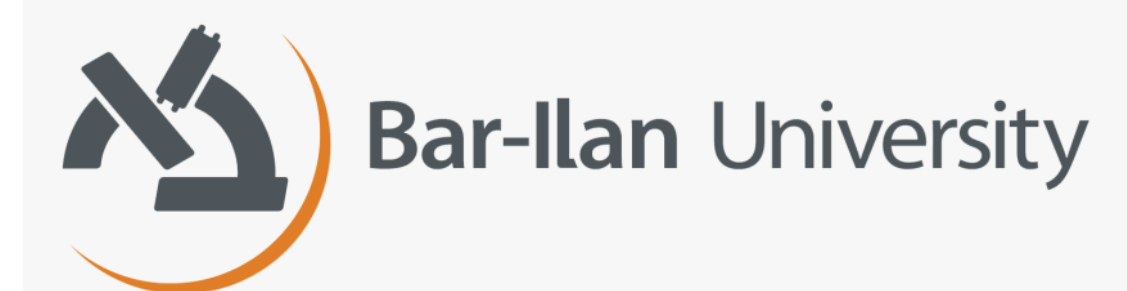


# Bit-precise Reasoning via Int-Blasting

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Mathias Preiner, Andrew Reynolds, Clark Barrett, Cesare Tinelli

Formal Reasoning about Financial Systems Workshop, 2022



# Bit-precise Reasoning

- Machine integers / Addresses
- Variables:  $x, y, z, \dots$
- Constants:  $0000, 01000010, 11111111, \dots$
- Relations:  $=, \text{bvult (unsigned), bvslt (signed), } \dots$
- BV Operators:  $\text{bvadd (+), bvmul } (\cdot), \text{bvand } (&), \text{bvshl } (\ll), \dots$
- Logical Operators:  $\wedge, \vee, \neg, \forall, \dots$
- All terms are **sorted**:  $\text{BV}[1], \text{BV}[2], \dots$



# Bit-vector Solving in SMT

- Bit-blasting (state-of-the-art)

- bits — Boolean variables

- operators — circuits

- Scalability problems:

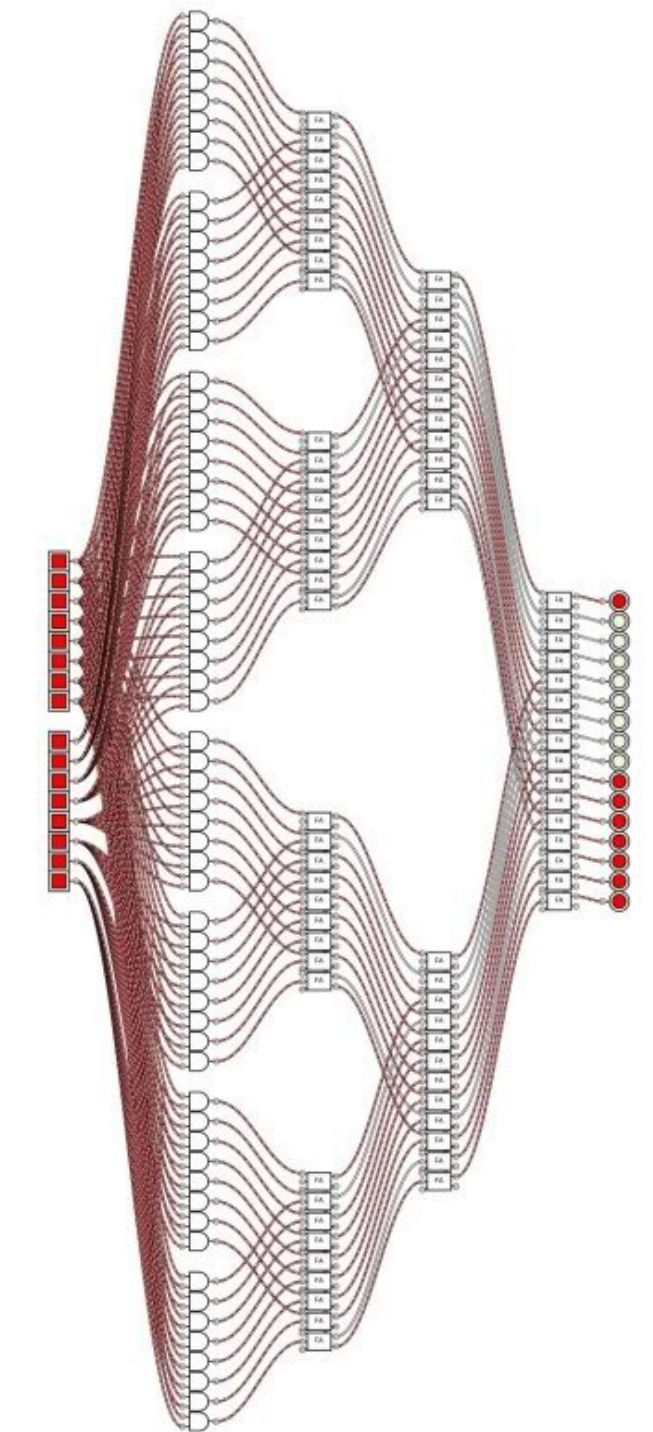
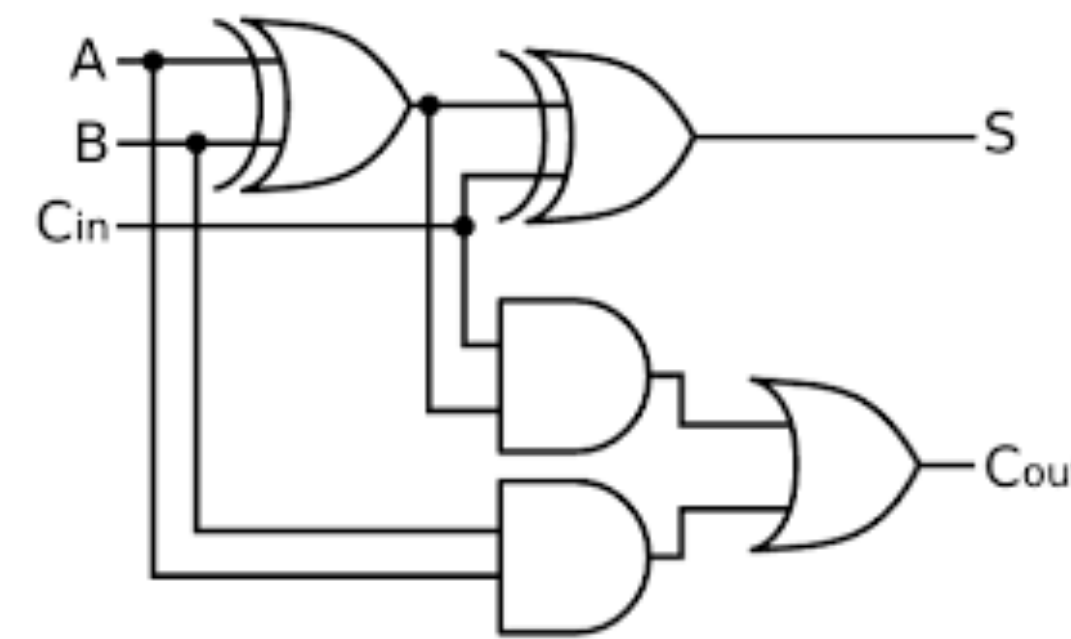
- Large bit-widths (e.g., 256)

- “Normal” bit-widths (e.g., 32) with multiplication/division

- MC-SAT

- Local Search

- Integer approaches



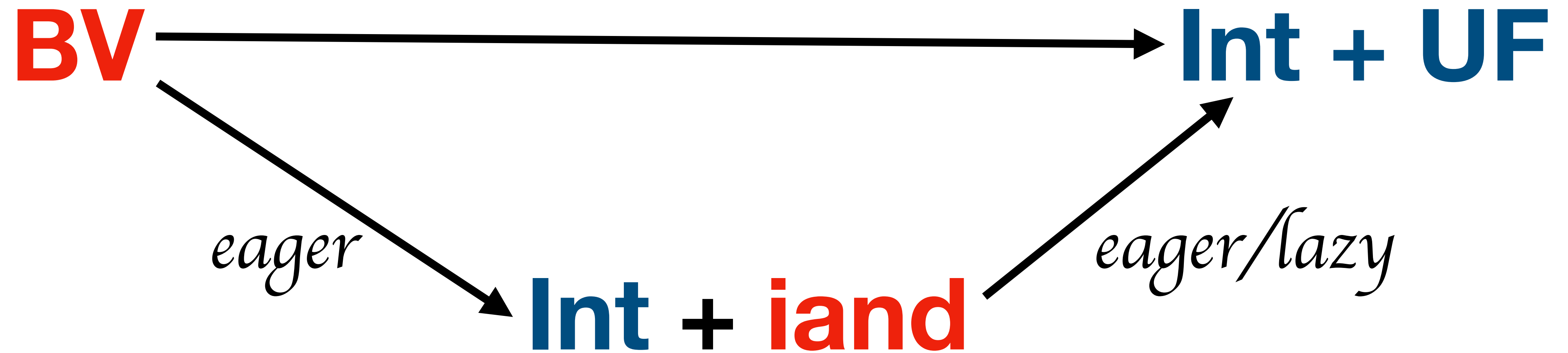
$$x + y \% 2^k$$

# Integers: Inside or Outside?

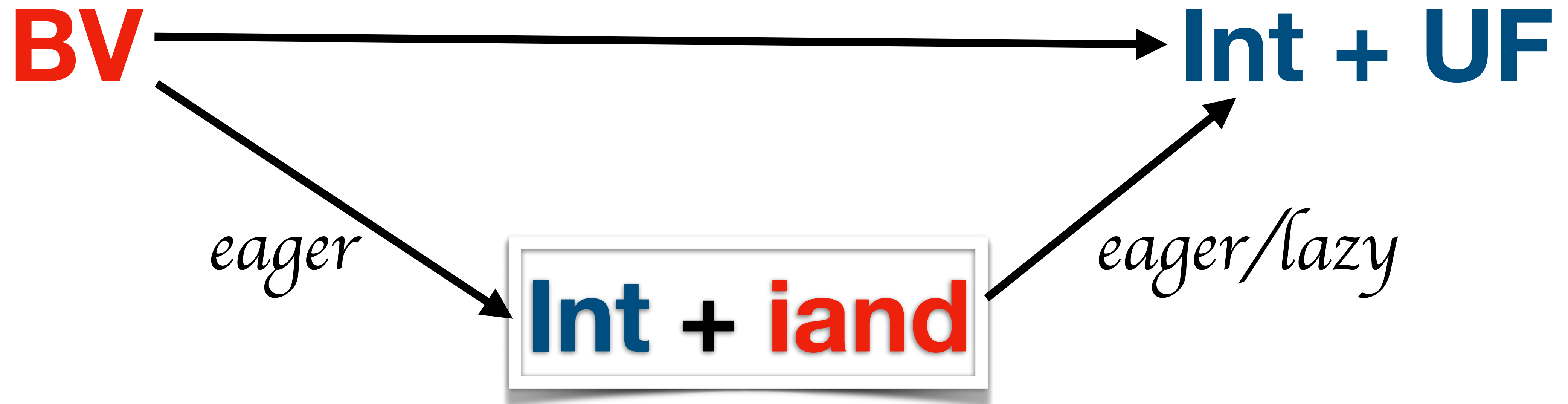


Application Level	Solver Level
Eager	<b>Flexible</b>
Abstract bit-wise operations	<b>Abstract/refine bit-wise operations</b>
Black box	<b>More control</b>
Application-specific	<b>General</b>

# Int-blasting

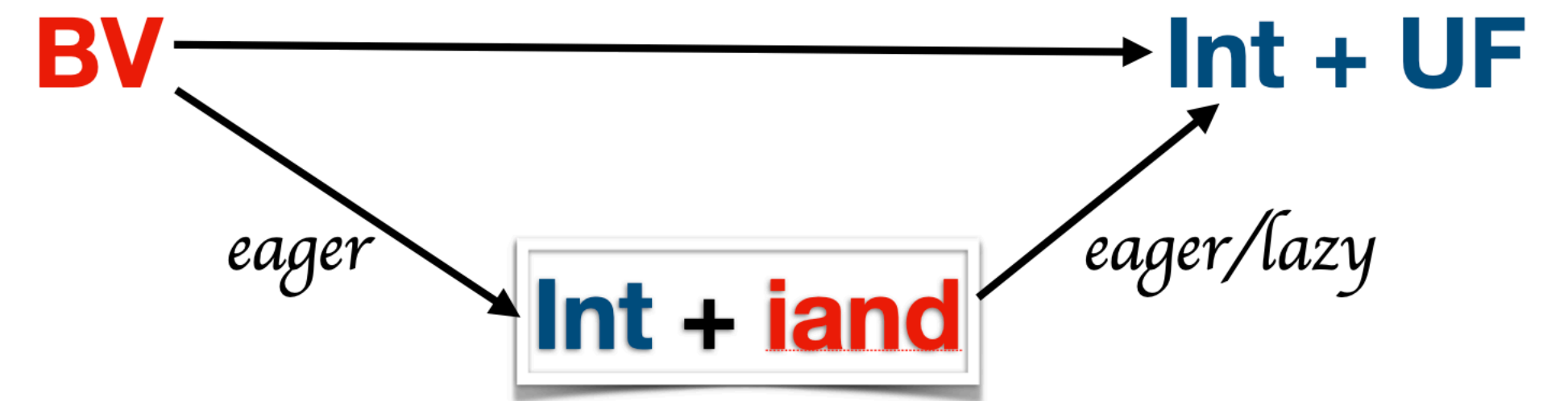


# Int-blasting



# Arith + iand

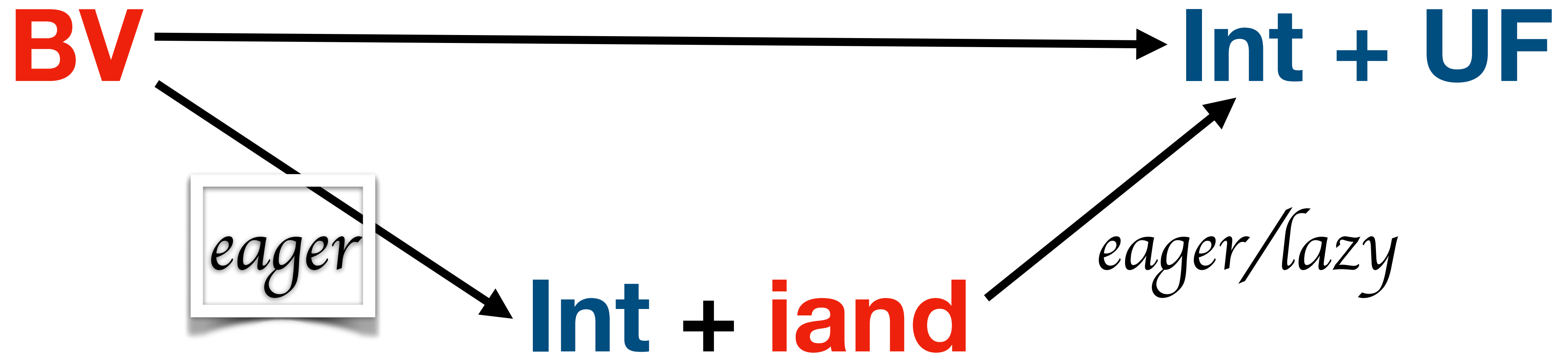
- Non-linear integer arithmetic
- iand
  - countably many binary operators  $\&_1, \&_2, \dots$
  - semantics of bit-wise “and”



$$\mathcal{Q}_4(1, 2) = 0$$

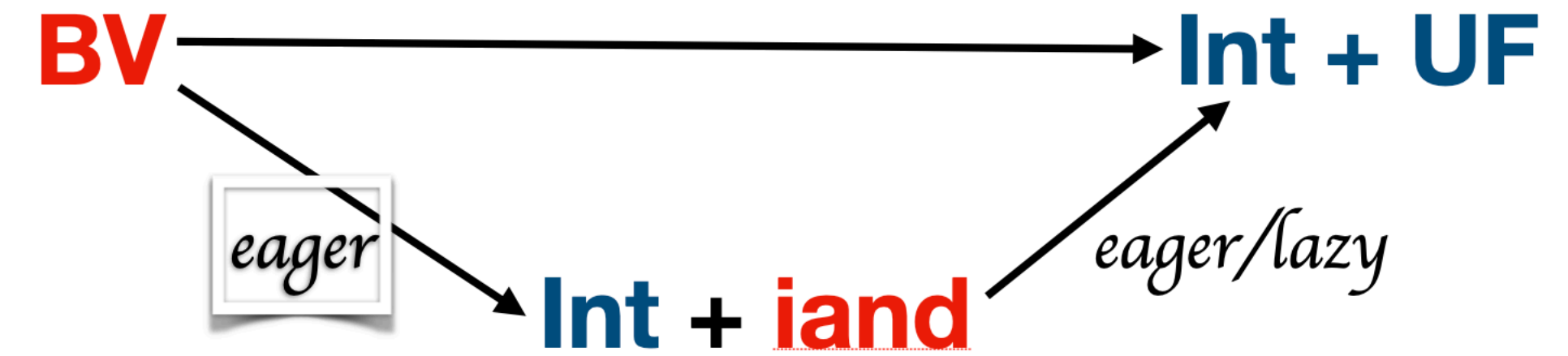
A handwritten bit-wise AND calculation for  $\mathcal{Q}_4(1, 2)$ . The number 1 is represented as 0001 and the number 2 as 0010. A horizontal line is drawn below these two numbers, and the result 0000 is written below the line. A red arrow points from the expression  $\mathcal{Q}_4(1, 2)$  down to the bit-wise AND calculation.

# Int-blasting





# BV $\longrightarrow$ Arith + iand



- BV variables  $\rightarrow$  Integer variables
- BV constants  $\rightarrow$  **unsigned** integer constants
- BV operators  $\rightarrow$  integer terms, based on **SMT-LIB**
- BV bit-wise “and”  $\rightarrow$  iand
- Some operators are eliminated

```
theory FixedSizeBitVectors

:smt-lib-version 2.6
:smt-lib-release "2017-11-24"
:written-by "Silvio Ranise, Cesare Tinelli, and Clark Barrett"
:date "2010-05-02"
:last-updated "2017-06-13"
:update-history
"Note: history only accounts for content changes, not release changes."
2020-05-20 Fixed minor typo
2017-06-13 Added :left-assoc attribute to bvand, bvor, bvadd,
2017-05-03 Updated to version 2.6; changed semantics of division and
remainder operators.
2016-04-20 Minor formatting of notes fields.
2015-04-25 Updated to Version 2.5.
2013-06-24 Renamed theory's name from Fixed_Size_Bit_Vectors to
FixedSizeBitVectors for consistency.
Added :value attribute.
"
```

$$x +_{\text{BV}} y \Rightarrow x' +_{\text{N}} y' \pmod{2^k}$$

**BV**  $\longrightarrow$  **Arith + iand**



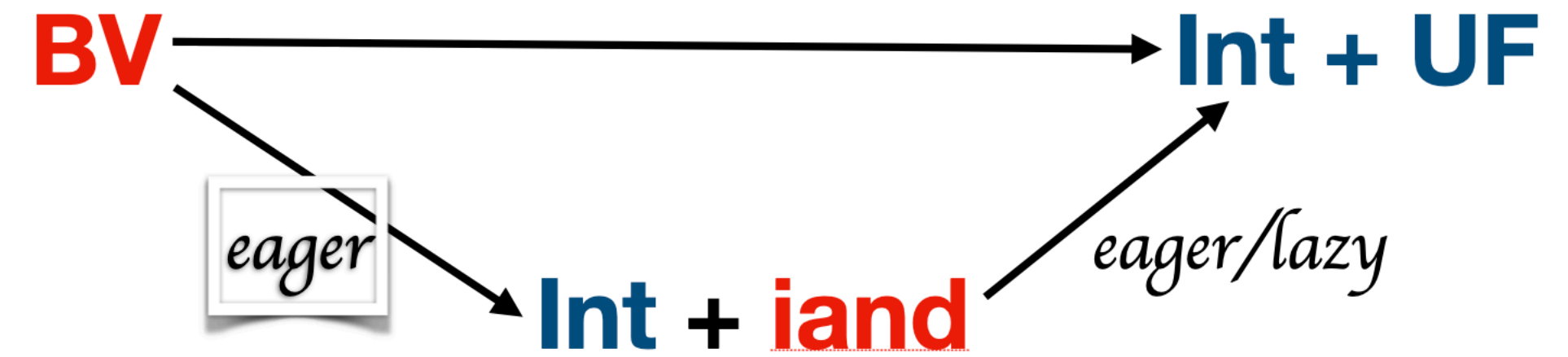
$$\frac{\mathcal{T} \varphi:}{\mathcal{C} \varphi \wedge \text{LEM}^{\leq}(\varphi)}$$

$\mathcal{C} e:$   
Match  $e:$

$$\begin{array}{ll} x & \rightarrow \chi(x) \\ c & \rightarrow [c]_{\mathbb{N}} \\ t_1 = t_2 & \rightarrow \mathcal{C} t_1 = \mathcal{C} t_2 \end{array}$$

$\chi$  is a 1-1 mapping between BV variables and integer variables  
 $[\cdot]_{\mathbb{N}}$  translates bit-vectors to unsigned integers

# BV $\longrightarrow$ Arith + iand



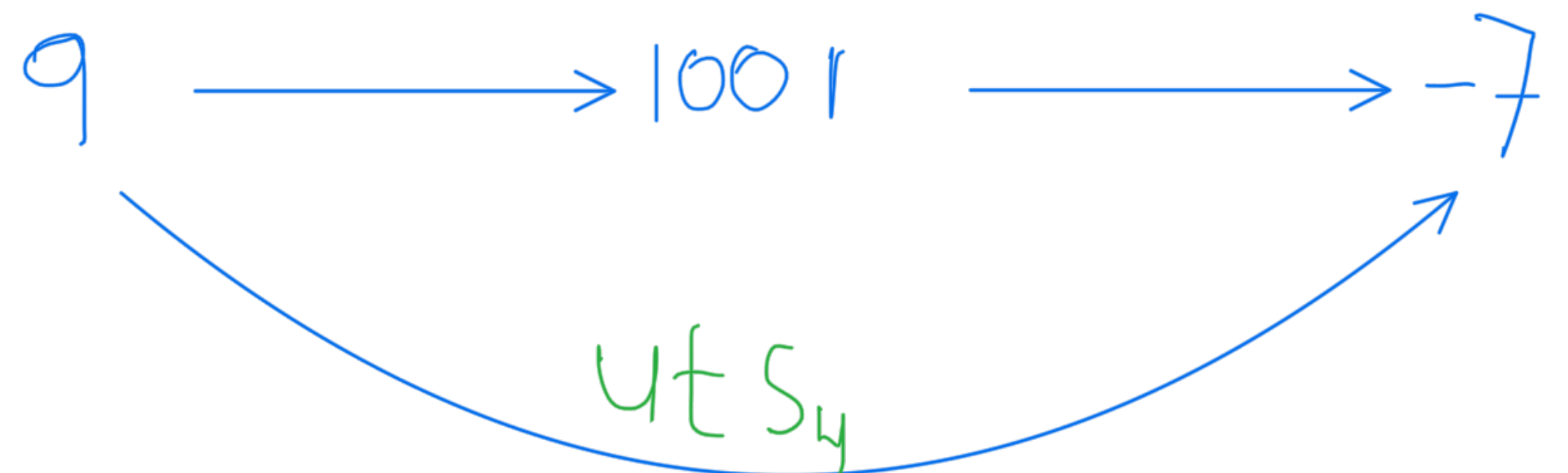
$$\frac{\mathcal{T} \varphi:}{\mathcal{C} \varphi \wedge \text{LEM}^{\leq}(\varphi)}$$

$\mathcal{C} e:$   
Match  $e:$

$$\begin{aligned} t_1 \bowtie^{\text{BV}} t_2 &\rightarrow \mathcal{C} t_1 \bowtie \mathcal{C} t_2 \\ t_1 \bowtie_s^{\text{BV}} t_2 &\rightarrow \text{uts}_k(\mathcal{C} t_1) \bowtie \text{uts}_k(\mathcal{C} t_2) \end{aligned}$$

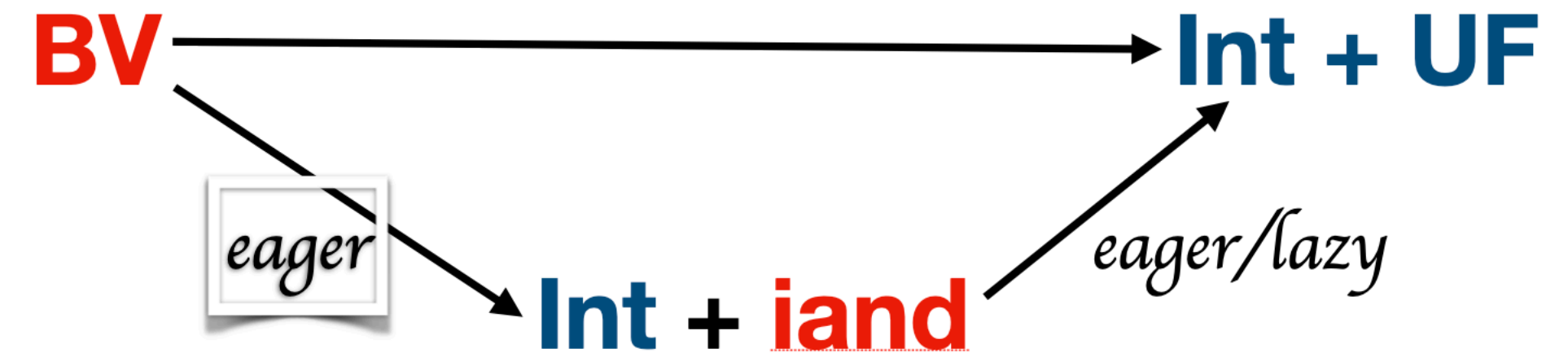
$$\bowtie \in \{ <, \leq, >, \geq \}$$

$\text{uts}_k(\cdot)$  : from unsigned to signed



$$\text{uts}_k(x) = 2 \cdot (x \bmod 2^{k-1}) - x$$

# BV $\longrightarrow$ Arith + iand



$$\frac{\mathcal{T} \varphi:}{\mathcal{C} \varphi \wedge \text{LEM}^{\leq}(\varphi)}$$

$\mathcal{C} e:$   
Match  $e:$

$$\begin{aligned} t_1 +^{\text{BV}} t_2 &\rightarrow (\mathcal{C} t_1 + \mathcal{C} t_2) \bmod 2^k \\ t_1 -^{\text{BV}} t_2 &\rightarrow (\mathcal{C} t_1 - \mathcal{C} t_2) \bmod 2^k \\ t_1 \cdot^{\text{BV}} t_2 &\rightarrow (\mathcal{C} t_1 \cdot \mathcal{C} t_2) \bmod 2^k \\ \sim^{\text{BV}} t_1 &\rightarrow 2^k - (\mathcal{C} t_1 + 1) \\ -^{\text{BV}} t_1 &\rightarrow (2^k - \mathcal{C} t_1) \bmod 2^k \end{aligned}$$

$k$  is the bit-width

## Example

$$-^{\text{BV}}(x +^{\text{BV}} y) = z$$



$$(2^k - (x' + y' \bmod 2^k)) \bmod 2^k = z'$$

**BV**  $\longrightarrow$  **Arith + iand**

$$\frac{\mathcal{T} \varphi:}{\mathcal{C} \varphi \wedge \text{LEM}^{\leq}(\varphi)}$$

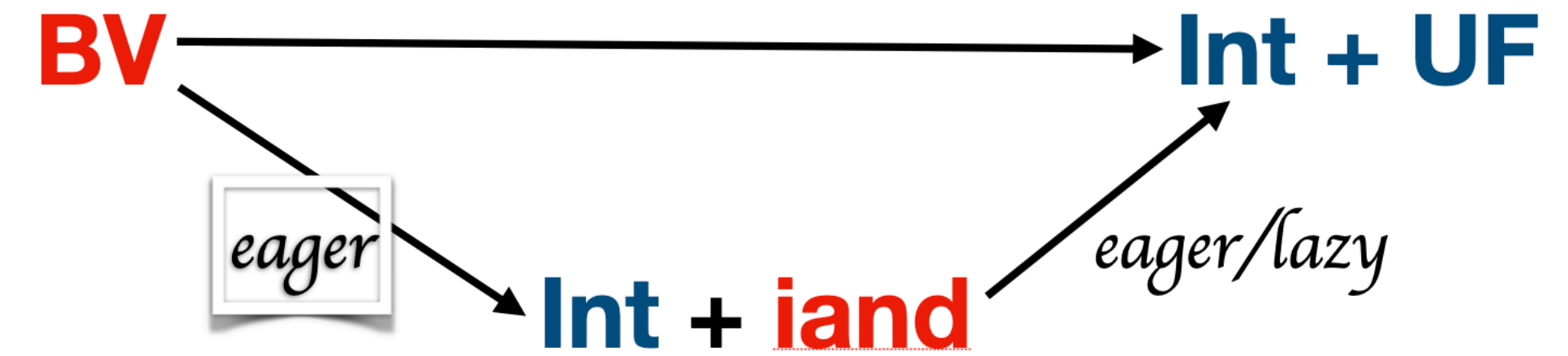
$\mathcal{C} e:$   
Match  $e:$

$$\begin{aligned} t_1 \text{ div}^{\text{BV}} t_2 &\rightarrow \text{ite}(\mathcal{C} t_2 = 0, 2^k - 1, \mathcal{C} t_1 \text{ div } \mathcal{C} t_2) \\ t_1 \text{ mod}^{\text{BV}} t_2 &\rightarrow \text{ite}(\mathcal{C} t_2 = 0, \mathcal{C} t_1, \mathcal{C} t_1 \text{ mod } \mathcal{C} t_2) \\ t_1 \circ^{\text{BV}} t_2 &\rightarrow \mathcal{C} t_1 \cdot 2^k + \mathcal{C} t_2 \\ t_1[u : l]^{\text{BV}} &\rightarrow \mathcal{C} t_1 \text{ div } 2^l \text{ mod } 2^{u-l+1} \end{aligned}$$



ite — if then else

**BV**  $\longrightarrow$  **Arith + iand**



$$\frac{\mathcal{T} \varphi:}{\mathcal{C} \varphi \wedge \text{LEM}^{\leq}(\varphi)}$$

$\mathcal{C} e:$   
Match  $e:$

$$\begin{aligned} t_1 \ll^{\text{BV}} t_2 &\quad \rightarrow \quad (\mathcal{C} t_1 \cdot \text{pow2}(\mathcal{C} t_2)) \bmod 2^k \\ t_1 \gg^{\text{BV}} t_2 &\quad \rightarrow \quad \mathcal{C} t_1 \text{ div } \text{pow2}(\mathcal{C} t_2) \end{aligned}$$

pow2 is eliminated using `ite`

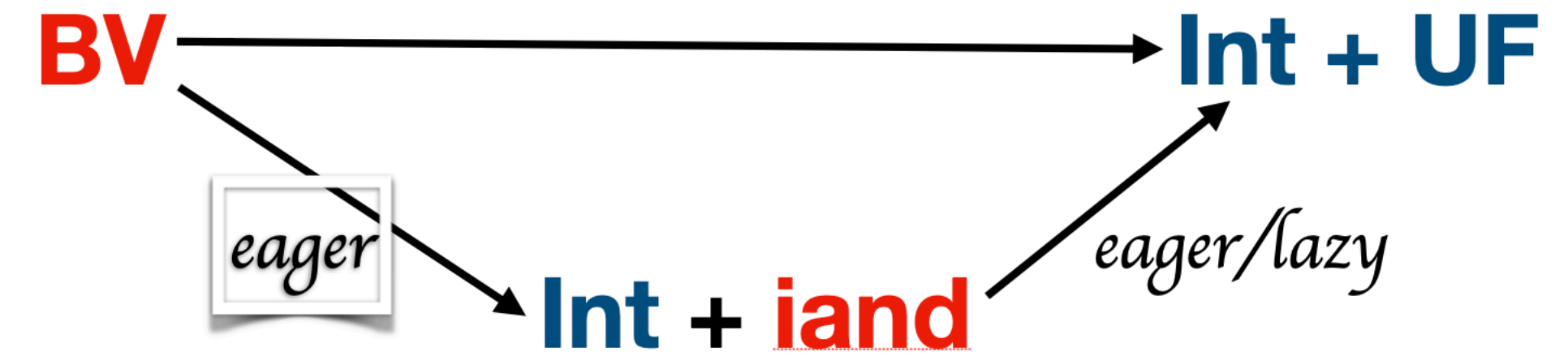
$$\text{pow2}(x) = \text{ite}(x = 0, 1, \text{ite}(x = 1, 2, \text{ite}(\dots, \text{ite}(x = k, 2^k, 0) \dots))$$

**BV**  $\longrightarrow$  **Arith + iand**

$$\frac{\mathcal{T} \varphi:}{\mathcal{C} \varphi \wedge \text{LEM}^{\leq}(\varphi)}$$

$\mathcal{C} e:$   
Match  $e:$

$$t_1 \&^{\text{BV}} t_2 \quad \longrightarrow \quad \&_k^{\mathbb{N}}(\mathcal{C} t_1, \mathcal{C} t_2)$$



$k$  is the bit-width

$\&_k^{\mathbb{N}}$  is an **iand** operator

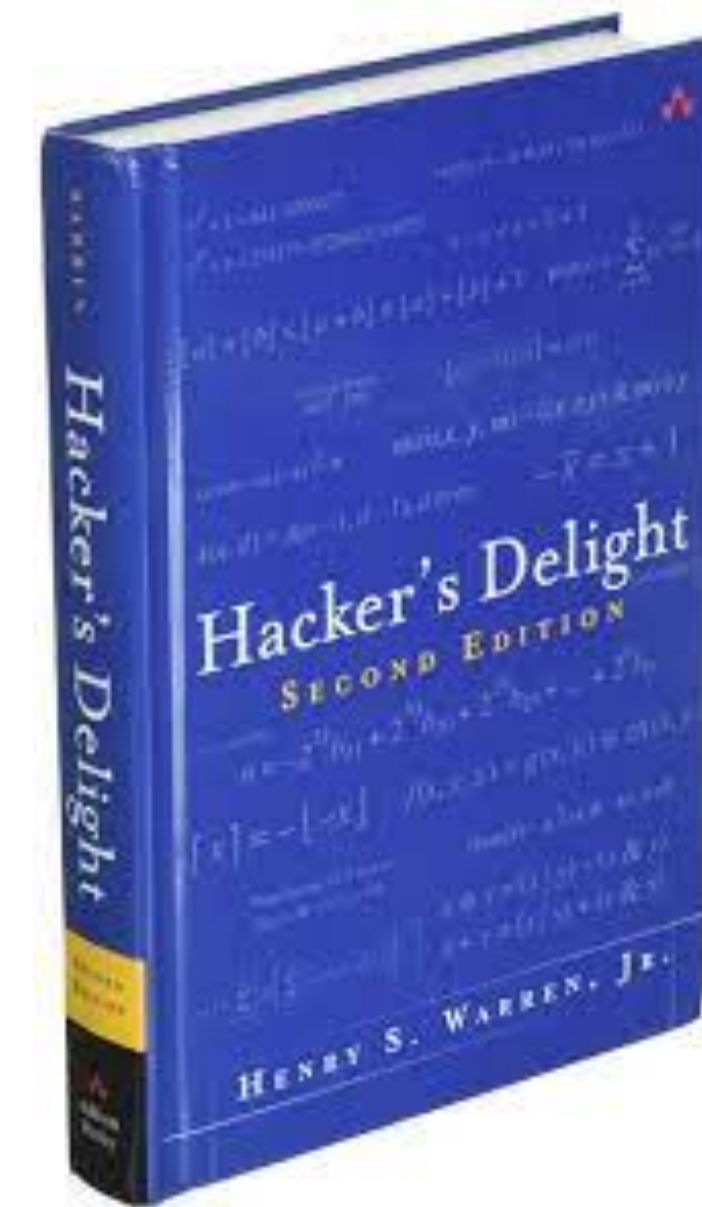
**BV**  $\longrightarrow$  **Arith + iand**

$$\frac{\mathcal{T} \varphi:}{\mathcal{C} \varphi \wedge \text{LEM}^{\leq}(\varphi)}$$

$\mathcal{C} e:$   
Match  $e:$

$$x \mid^{\text{BV}} y = (x +^{\text{BV}} y) -^{\text{BV}} (x \&^{\text{BV}} y)$$

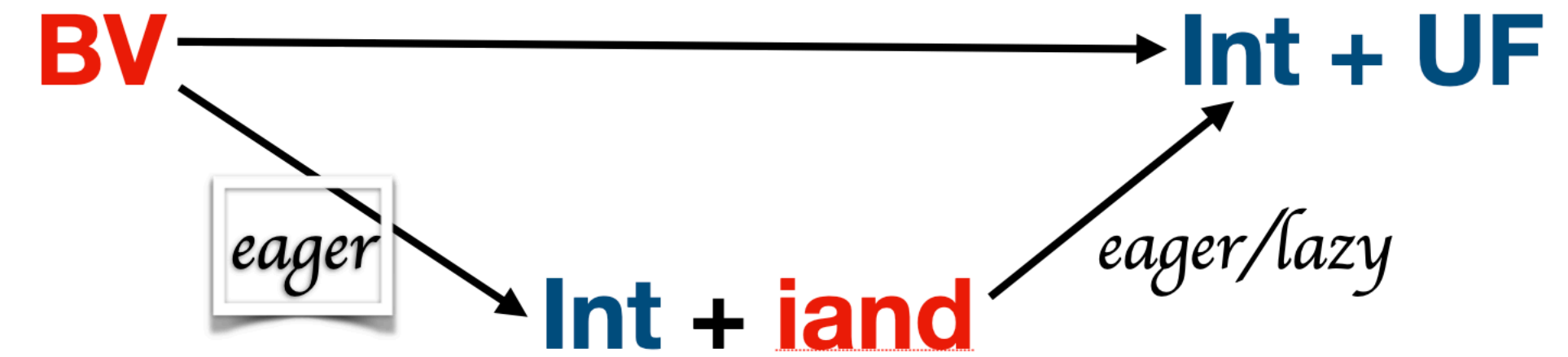
$$x \oplus^{\text{BV}} y = (x \mid^{\text{BV}} y) -^{\text{BV}} (x \&^{\text{BV}} y)$$



bvor and bvxor are eliminated



# BV $\longrightarrow$ Arith + iand



$$\frac{\mathcal{T} \varphi:}{\mathcal{C} \varphi \wedge \text{LEM}^{\leq}(\varphi)}$$

$\text{LEM}^{\leq}(e)$ :  
Match  $e$ :

$$x \quad \rightarrow \quad 0 \leq \chi(x) < 2^{\kappa(x)}$$

$$c \quad \rightarrow \quad \top$$

$$t_1 = t_2 \quad \rightarrow \quad \text{LEM}^{\leq}(t_1) \wedge \text{LEM}^{\leq}(t_2)$$

$$f^{\text{BV}}(t_1, t_2) \quad \rightarrow \quad 0 \leq \&_k^{\mathbb{N}}(\mathcal{C} t_1, \mathcal{C} t_2) < 2^k \wedge \text{LEM}^{\leq}(t_1) \wedge \text{LEM}^{\leq}(t_2)$$

$$g^{\text{BV}}(t_1, \dots, t_n) \quad \rightarrow \quad \bigwedge_{i=1}^n \text{LEM}^{\leq}(t_i)$$

$$\diamond(\varphi_1, \dots, \varphi_n) \quad \rightarrow \quad \bigwedge_{i=1}^n \text{LEM}^{\leq}(\varphi_i)$$

$\text{LEM}^{\leq}$  includes range constraints  $0 \leq t < 2^k$

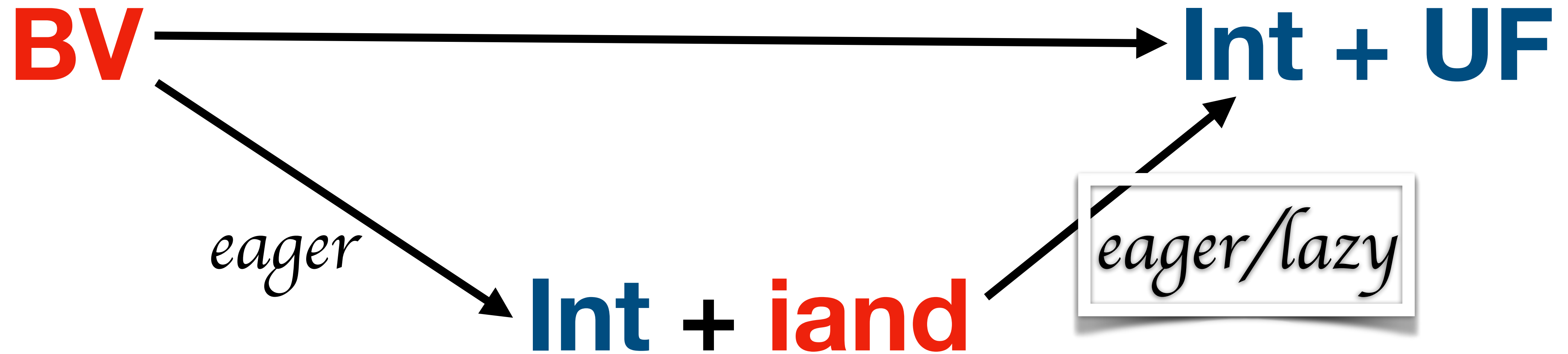
$$f^{\text{BV}} \in \{ \&^{\text{BV}}, \text{BV}, \oplus^{\text{BV}} \}$$

$g^{\text{BV}}$  : other BV operators

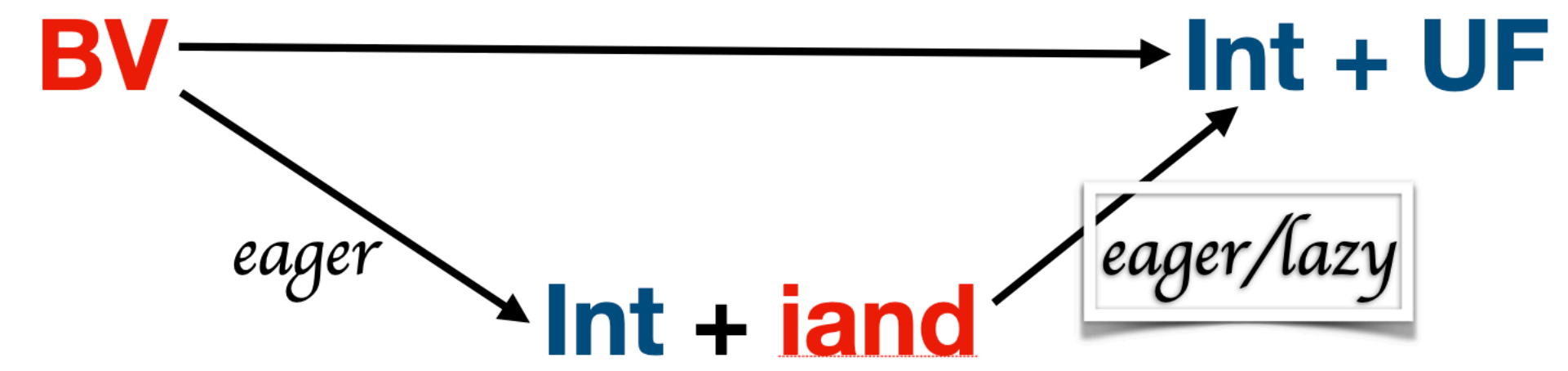
$\diamond$  : Boolean operators

$\chi$  maps BV variables to integer variables

# Int-blasting



Arith + iand  $\longrightarrow$  Arith + UF



	Sum	Bitwise
Eager	$\wedge (\Sigma(\dots) = \dots)$	$\wedge \wedge (\dots = \dots)$
Lazy	$\Sigma(\dots) = \dots$	$\wedge (\dots = \dots)$
	$\Sigma(\dots) = \dots$	$\wedge (\dots = \dots)$
	$\Sigma(\dots) = \dots$	$\wedge (\dots = \dots)$

# Arith + iand $\longrightarrow$ Arith + UF

## Eager Version

$\mathcal{T}_A \varphi$ :

$\text{LEM}_A^{\&}(\varphi) \wedge \varphi$

$\underline{\text{LEM}_A^{\&}}(e)$ :

Match  $e$ :

$x \rightarrow \top$

$c \rightarrow \top$

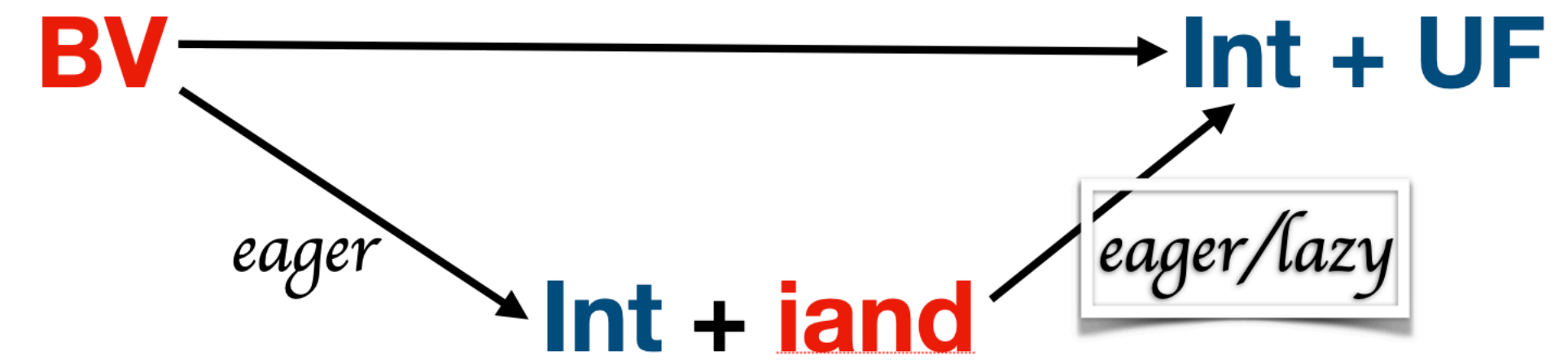
$t_1 = t_2 \rightarrow \text{LEM}_A^{\&}(t_1) \wedge \text{LEM}_A^{\&}(t_2)$

$\diamond(\varphi_1, \dots, \varphi_n) \rightarrow \bigwedge_{i=1}^n \text{LEM}_A^{\&}(\varphi_i)$

$f(t_1, \dots, t_n) \rightarrow \bigwedge_{i=1}^n \text{LEM}_A^{\&}(t_i)$

$\&_k^{\mathbb{N}}(t_1, t_2) \rightarrow \boxed{\text{IAND}_A(t_1, t_2)} \wedge \bigwedge_{i \in \{1, 2\}} \text{LEM}_A^{\&}(t_i)$

$A \in \{\text{sum, bitwise}\}$



# Arith + iand $\longrightarrow$ Arith + UF

## Eager-sum Version

$\mathcal{T}_A \varphi$ :

$$\text{LEM}_A^{\&}(\varphi) \wedge \varphi$$

$\text{LEM}_A^{\&}(e)$ :

Match  $e$ :

$$x \quad \rightarrow \top$$

$$c \quad \rightarrow \top$$

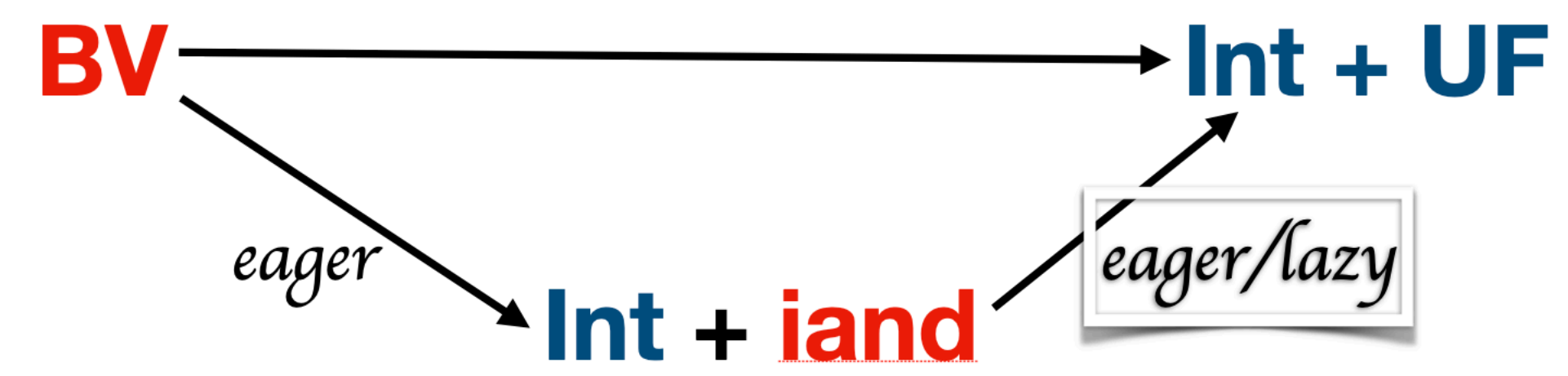
$$t_1 = t_2 \quad \rightarrow \text{LEM}_A^{\&}(t_1) \wedge \text{LEM}_A^{\&}(t_2)$$

$$\diamond(\varphi_1, \dots, \varphi_n) \rightarrow \bigwedge_{i=1}^n \text{LEM}_A^{\&}(\varphi_i)$$

$$f(t_1, \dots, t_n) \rightarrow \bigwedge_{i=1}^n \text{LEM}_A^{\&}(t_i)$$

$$\&_k^{\mathbb{N}}(t_1, t_2) \rightarrow \boxed{\text{IAND}_A(t_1, t_2)} \wedge \bigwedge_{i \in \{1,2\}} \text{LEM}_A^{\&}(t_i)$$

$A \in \{\text{sum, bitwise}\}$



$\text{IAND}_{\text{sum}}(t_1, t_2)$ :

$$\&_k^{\mathbb{N}}(t_1, t_2) = \sum_{i=0}^{k-1} 2^i \cdot \text{ITE}(a_i, b_i)$$

$$a_i = t_1 \text{ div } 2^i \text{ mod } 2$$

$$b_i = t_2 \text{ div } 2^i \text{ mod } 2$$

$$\text{ITE}(x, y) = \text{ite}(x = y = 1, 1, 0)$$

$a_i$  : ith bit of  $t_1$

$b_i$  : ith bit of  $t_2$

# Arith + iand $\longrightarrow$ Arith + UF

## Eager-bitwise Version

$\mathcal{T}_A \varphi$ :

$$\text{LEM}_A^{\&}(\varphi) \wedge \varphi$$

$\text{LEM}_A^{\&}(e)$ :

Match  $e$ :

$$x \quad \rightarrow \top$$

$$c \quad \rightarrow \top$$

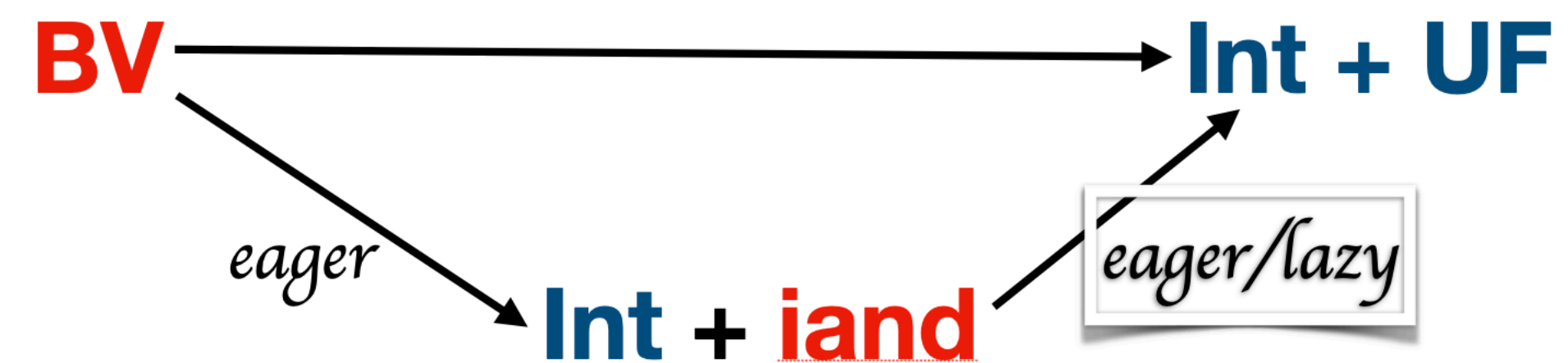
$$t_1 = t_2 \quad \rightarrow \text{LEM}_A^{\&}(t_1) \wedge \text{LEM}_A^{\&}(t_2)$$

$$\diamond(\varphi_1, \dots, \varphi_n) \rightarrow \bigwedge_{i=1}^n \text{LEM}_A^{\&}(\varphi_i)$$

$$f(t_1, \dots, t_n) \rightarrow \bigwedge_{i=1}^n \text{LEM}_A^{\&}(t_i)$$

$$\&_k^{\mathbb{N}}(t_1, t_2) \rightarrow \boxed{\text{IAND}_A(t_1, t_2)} \wedge \bigwedge_{i \in \{1,2\}} \text{LEM}_A^{\&}(t_i)$$

$A \in \{\text{sum, bitwise}\}$



$\text{IAND}_{\text{bitwise}}(t_1, t_2)$ :

$$\bigwedge_{i=0}^{k-1} c_i = \text{ITE}(a_i, b_i)$$

$$a_i = t_1 \text{ div } 2^i \text{ mod } 2$$

$$b_i = t_2 \text{ div } 2^i \text{ mod } 2$$

$$c_i = \&_k^{\mathbb{N}}(t_1, t_2) \text{ div } 2^i \text{ mod } 2$$

$$\text{ITE}(x, y) = \text{ite}(x = y = 1, 1, 0)$$

# Arith + iand $\longrightarrow$ Arith + UF

## Lazy Versions

$$\Gamma := \{ \mathcal{T} \varphi \}$$

$$\Delta := \{ \&_k^{\mathbb{N}}(t_1, t_2) \mid \&_k^{\mathbb{N}}(t_1, t_2) \text{ occurs in } \mathcal{T} \varphi \}$$

$$\Lambda := \text{Prop}(\Delta) \cup \{ \text{IAND}_A(t_1, t_2) \mid \&_k^{\mathbb{N}}(t_1, t_2) \in \Delta \}$$

Repeat:

1. If  $P_{T_{\text{IAUF}}}(\bigwedge \Gamma)$  is “unsat”, then return “unsat”.

2. Otherwise, let  $\mathcal{I} = P_{T_{\text{IAUF}}}(\bigwedge \Gamma)$

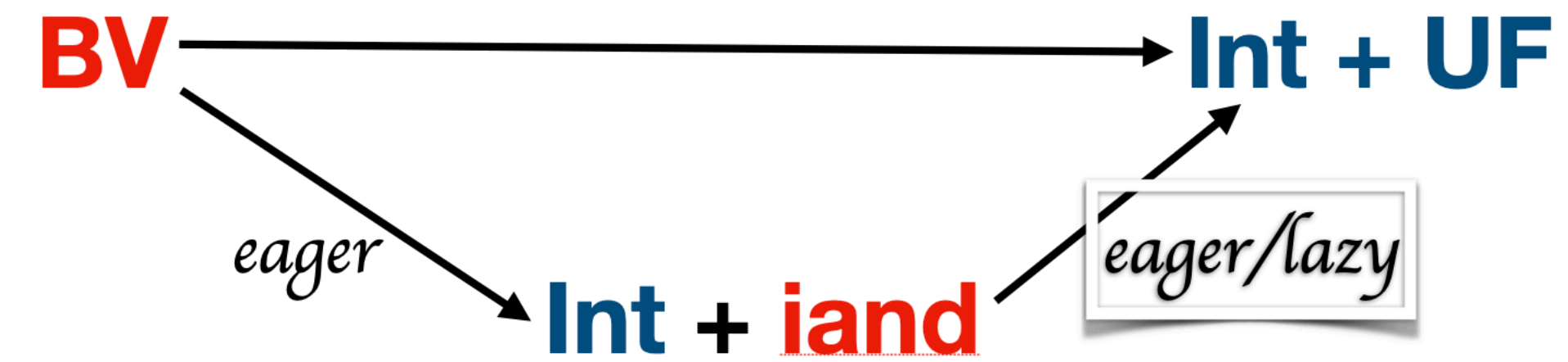
*/\* check  $\mathcal{I}$  against properties of  $\&_k^{\mathbb{N}}$  \*/*

(a) If  $\mathcal{I}$  satisfies  $\Lambda$ , return “sat”.

(b) Otherwise:

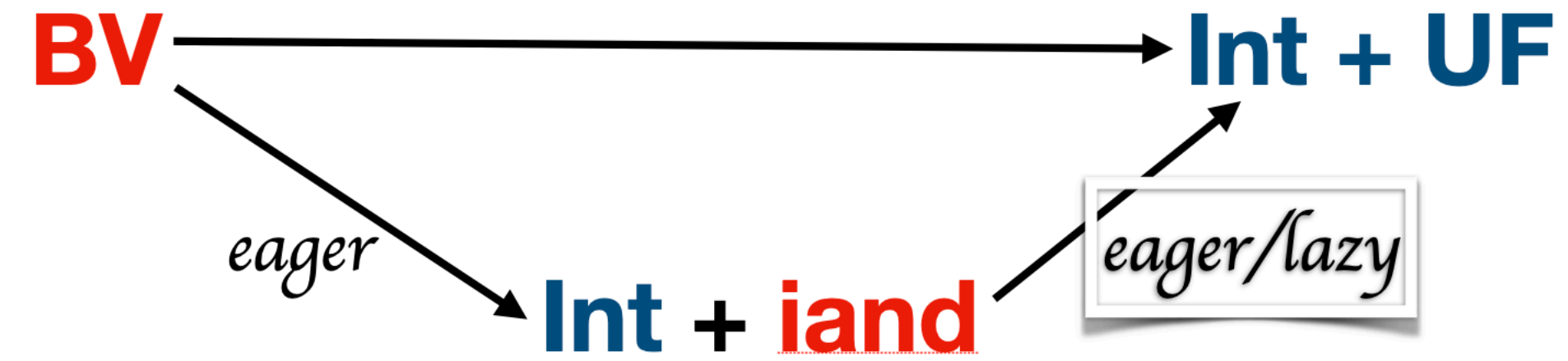
*/\* refine abstraction  $\Gamma$  \*/*

$$\Gamma := \Gamma \cup \{ \psi \in \Lambda \mid \mathcal{I} \not\models \psi \}$$



# Arith + iand $\longrightarrow$ Arith + UF

## Lazy Versions



$$\Gamma := \{ \mathcal{T} \varphi \}$$

$$\Delta := \{ \&_k^{\mathbb{N}}(t_1, t_2) \mid \&_k^{\mathbb{N}}(t_1, t_2) \text{ occurs in } \mathcal{T} \varphi \}$$

$$\Lambda := \text{Prop}(\Delta) \cup \{ \text{IAND}_A(t_1, t_2) \mid \&_k^{\mathbb{N}}(t_1, t_2) \in \Delta \}$$

Repeat:

1. If  $P_{T_{\text{IAUF}}}(\bigwedge \Gamma)$  is “unsat”, then return “unsat”.

2. Otherwise, let  $\mathcal{I} = P_{T_{\text{IAUF}}}(\bigwedge \Gamma)$

*/\* check  $\mathcal{I}$  against properties of  $\&_k^{\mathbb{N}}$  \*/*

(a) If  $\mathcal{I}$  satisfies  $\Lambda$ , return “sat”.

(b) Otherwise:

*/\* refine abstraction  $\Gamma$  \*/*

$$\Gamma := \Gamma \cup \{ \psi \in \Lambda \mid \mathcal{I} \not\models \psi \}$$

$$\text{Prop}(\Delta) = \{ \text{Prop}(t_1, t_2) \mid \&_k^{\mathbb{N}}(t_1, t_2) \in \Delta \}$$

$\text{Prop}(t_1, t_2)$ :

$$\&_k^{\mathbb{N}}(t_1, t_2) \leq t_1 \wedge \&_k^{\mathbb{N}}(t_1, t_2) \leq t_2 \wedge \quad \text{bounds}$$

$$(t_1 = t_2 \Rightarrow \&_k^{\mathbb{N}}(t_1, t_2) = t_1) \wedge \quad \text{idempotence}$$

$$\&_k^{\mathbb{N}}(t_1, t_2) = \&_k^{\mathbb{N}}(t_2, t_1) \wedge \quad \text{symmetry}$$

$$\left. \begin{array}{l} (t_1 = 0 \Rightarrow \&_k^{\mathbb{N}}(t_1, t_2) = 0) \wedge \\ (t_1 = 2^k - 1 \Rightarrow \&_k^{\mathbb{N}}(t_1, t_2) = t_2) \wedge \\ (t_2 = 0 \Rightarrow \&_k^{\mathbb{N}}(t_1, t_2) = 0) \wedge \\ (t_2 = 2^k - 1 \Rightarrow \&_k^{\mathbb{N}}(t_1, t_2) = t_1) \end{array} \right\} \quad \text{special cases}$$

IAND<sub>sum</sub>( $t_1, t_2$ ):

$$\&_k^{\mathbb{N}}(t_1, t_2) = \sum_{i=0}^{k-1} 2^i \cdot \text{ITE}(a_i, b_i)$$

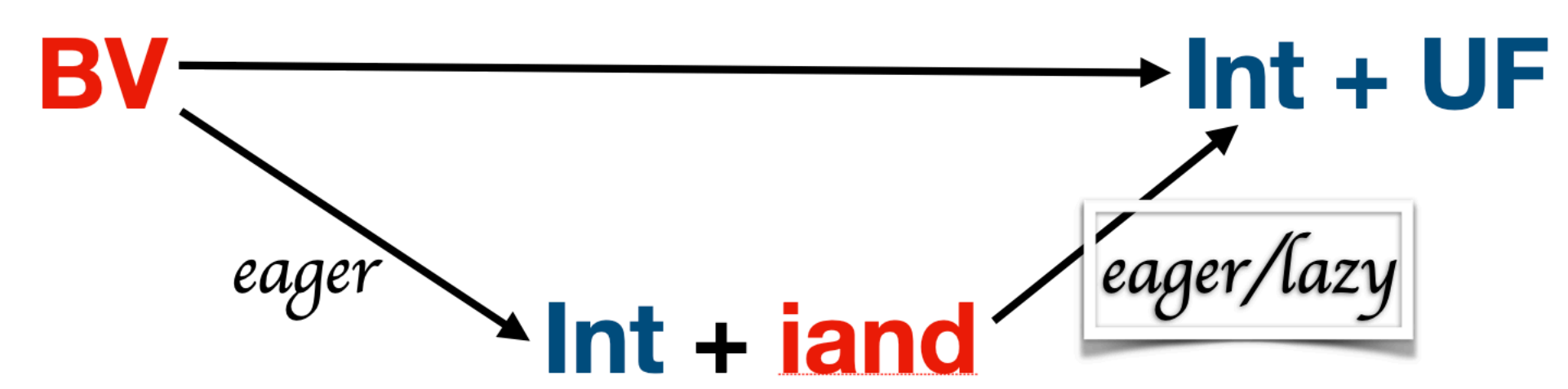
IAND<sub>bitwise</sub>( $t_1, t_2$ ):

$$\bigwedge_{i=0}^{k-1} c_i = \text{ITE}(a_i, b_i)$$

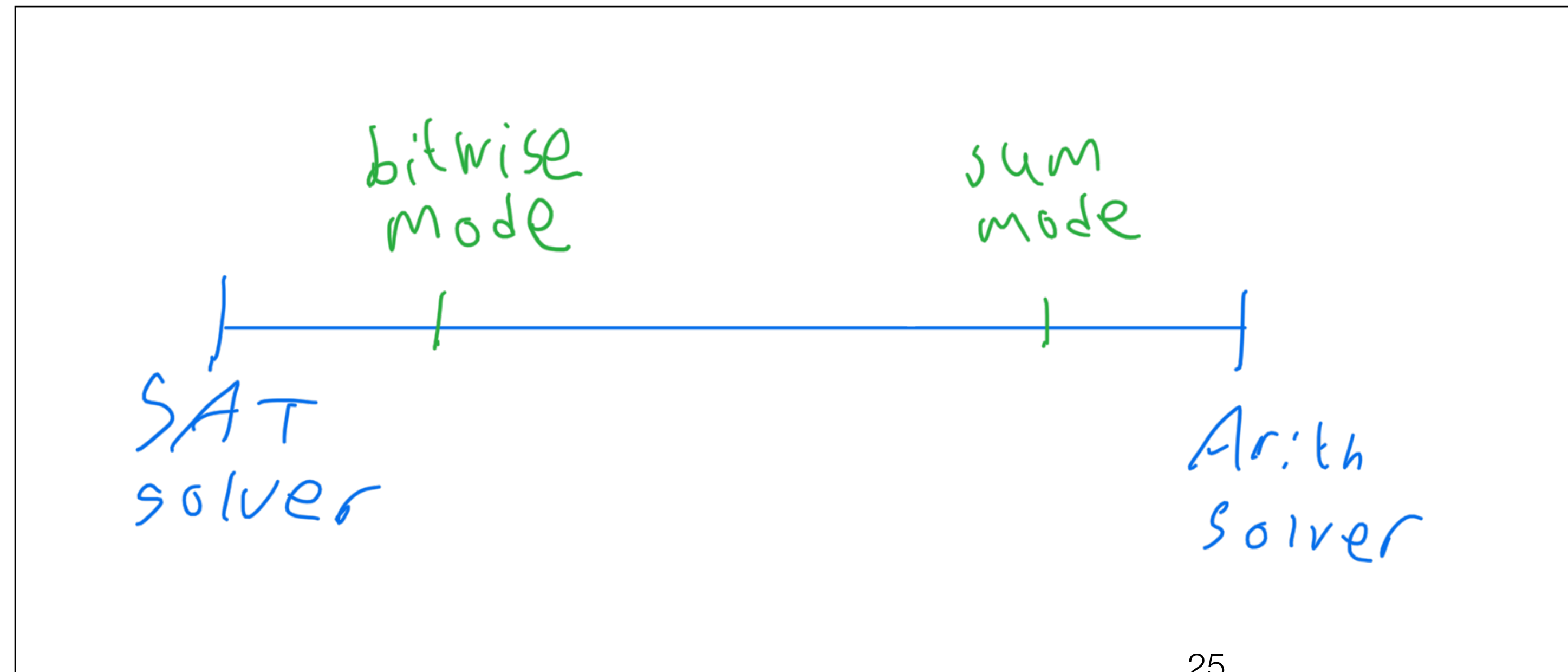
$P_{T_{\text{IAUF}}}$  is a UFNIA solver



# Arith + iand $\longrightarrow$ Arith + UF



- Both modes utilize the SAT-solver and Arith-solver
  - “The  $i$ th bit of  $x$ ” –  $(x \text{ div } 2^i) \text{ mod } 2$
- *bitwise* mode relies more on the **SAT-solver**
- *sum* mode relies more on the **Arith-solver**



	Sum	Bitwise
Eager	$\wedge (\Sigma(\dots) = \dots)$	$\wedge \wedge (\dots = \dots)$
Lazy	$\Sigma(\dots) = \dots$	$\wedge (\dots = \dots)$
	$\Sigma(\dots) = \dots$	$\wedge (\dots = \dots)$
	$\Sigma(\dots) = \dots$	$\wedge (\dots = \dots)$

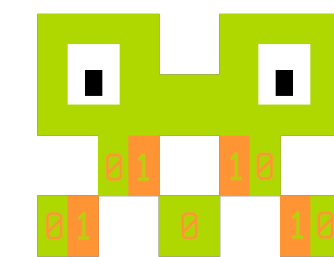
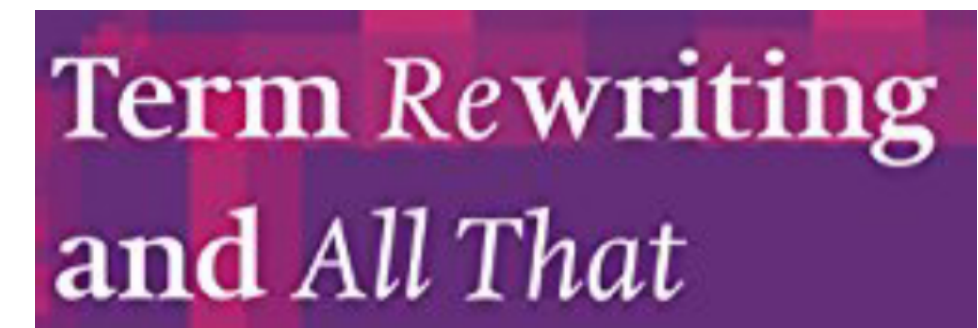
# Evaluation

Int-blasting is implemented in cvc5 (successor of CVC4)



# Evaluation

- Other tools:
  - Bitwuzla — first place in QF\_BV 2020
  - Yices — second place in QF\_BV 2020
  - cvc5 eager bit-blaster — baseline
  - (bw-ind — our integer-based bit-width independent prototype)
- Benchmarks:
  - SMT-LIB
  - Rewrite-rule Candidates
  - Certora Smart Contracts Verification



Yices2

cvc5

# SMT-LIB

- QF\_BV family
- 41,713 benchmarks
- Very diverse
- Not many large bit-widths



# Results – SMTLIB

- Timeout: 10 minutes
- Not competitive on SMT-LIB
  - Expected – Bit-blasting is state of the art
- Better on UNSAT than on SAT
  - Expected – Lemmas are aimed at finding conflicts

	SMT-LIB				ECRW				SC			
	<i>slvd</i>	<i>sat</i>	<i>uns</i>	<i>m</i>	<i>slvd</i>	<i>sat</i>	<i>uns</i>	<i>m</i>	<i>slvd</i>	<i>sat</i>	<i>uns</i>	<i>m</i>
<i>eager<sub>b</sub></i>	35031	10447	24584	38	41989	119	41870	0	<b>24</b>	9	15	0
<i>eager<sub>s</sub></i>	35035	10459	24576	28	41435	119	41316	77	<b>24</b>	9	15	0
<i>lazy<sub>b</sub></i>	35001	10383	24618	23	<b>47071</b>	119	46952	0	<b>24</b>	9	15	0
<i>lazy<sub>s</sub></i>	34819	10297	24522	27	45350	119	45231	138	<b>24</b>	9	15	0
<i>Bitwuzla</i>	41220	14233	26987	19	37297	265	37032	11120	16	8	8	0
<i>cvc5</i>	40543	14204	26339	36	33187	220	32967	17535	-	-	-	-
<i>Yices</i>	<b>41228</b>	14280	26948	11	31646	255	31391	15801	9	3	6	0
<i>bw-ind</i>	-	-	-	-	25608	0	25608	0	-	-	-	-

# Rewrite Rule Candidates

- **Hand-crafted** but represents a real application — rewrite rules for SMT-solvers
- Benchmark generation using SyGuS:
  - Synthesize pairs of terms that are equivalent for bit-width 4
  - Prove correctness for larger bit-widths
- Benchmarks:
  - **5491** equivalence checks
  - Each one instantiated with **10** bit-widths (16, 32, ... 8192)
  - Total **54,910** benchmarks

Term Rewriting  
and All That

# Results – Rewrite Rules

- Timeout: 5 minutes
- All int-blasting approaches are better
- Best int-blasting approach: lazy bitwise

	SMT-LIB				ECRW				SC			
	<i>slvd</i>	<i>sat</i>	<i>uns</i>	<i>m</i>	<i>slvd</i>	<i>sat</i>	<i>uns</i>	<i>m</i>	<i>slvd</i>	<i>sat</i>	<i>uns</i>	<i>m</i>
<i>eager<sub>b</sub></i>	35031	10447	24584	38	41989	119	41870	0	<b>24</b>	9	15	0
<i>eager<sub>s</sub></i>	35035	10459	24576	28	41435	119	41316	77	<b>24</b>	9	15	0
<i>lazy<sub>b</sub></i>	35001	10383	24618	23	<b>47071</b>	119	46952	0	<b>24</b>	9	15	0
<i>lazy<sub>s</sub></i>	34819	10297	24522	27	45350	119	45231	138	<b>24</b>	9	15	0
<i>Bitwuzla</i>	41220	14233	26987	19	37297	265	37032	11120	16	8	8	0
<i>cvc5</i>	40543	14204	26339	36	33187	220	32967	17535	-	-	-	-
<i>Yices</i>	<b>41228</b>	14280	26948	11	31646	255	31391	15801	9	3	6	0
<i>bw-ind</i>	-	-	-	-	25608	0	25608	0	-	-	-	-

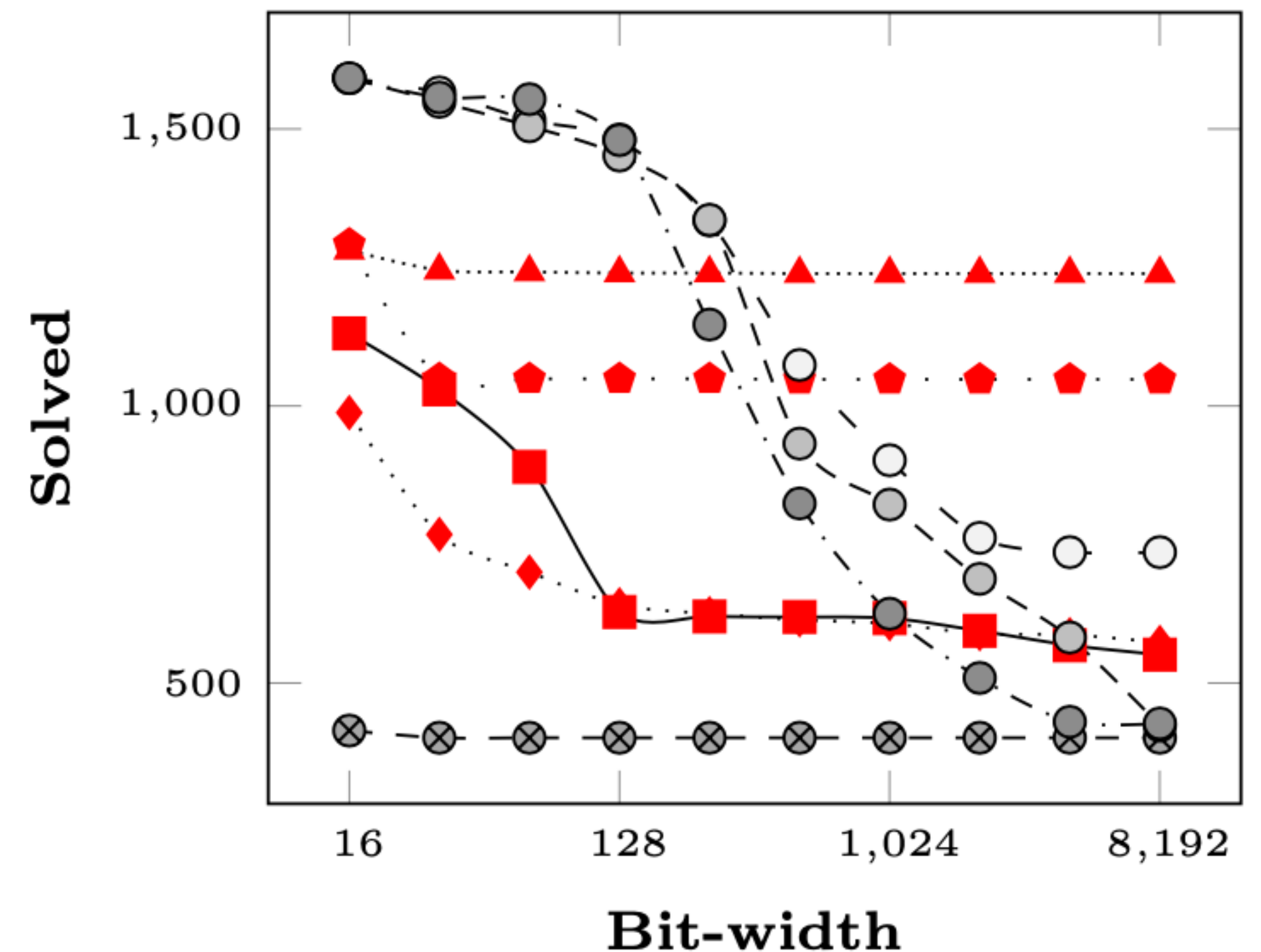
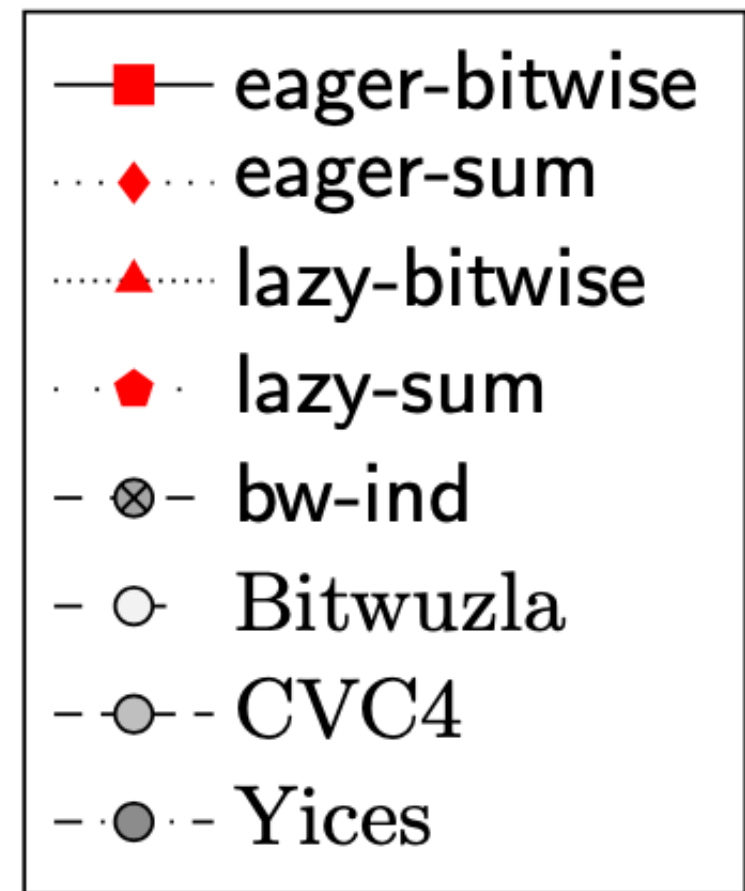
Term Rewriting  
and All That

# Results — Rewrite Rules

## With bvand

- with bvand: best starting from bit-width 512
- int-blasting approaches differ
- Lazy approaches are bit-width independent

Term Rewriting  
and All That



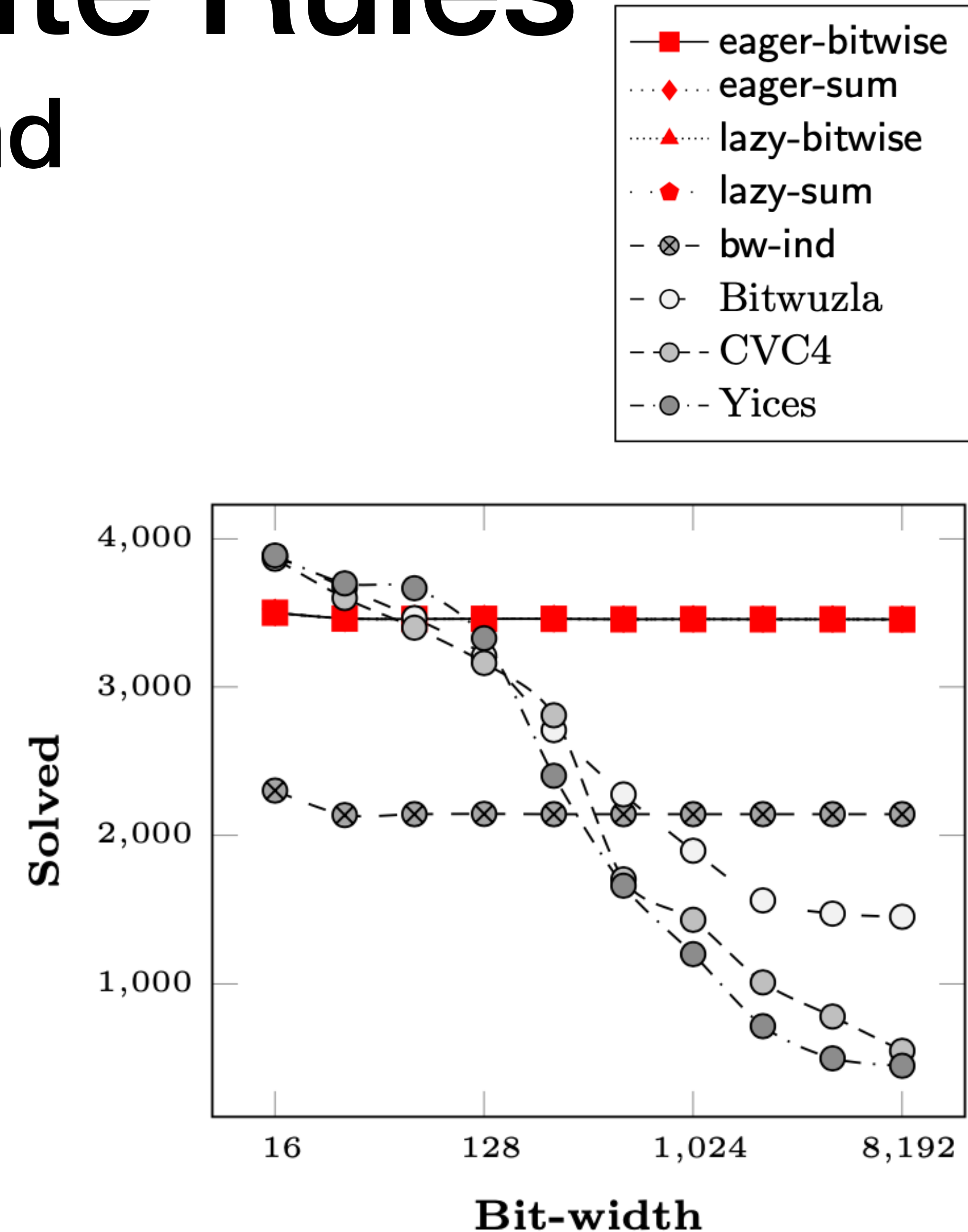


# Results — Rewrite Rules

## Without bvand

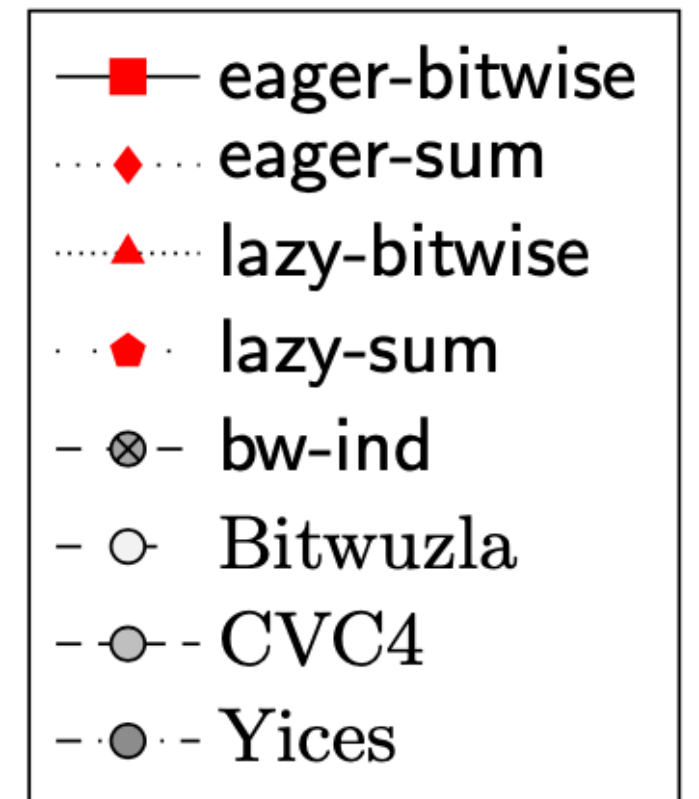
- with bvand: best starting from bit-width 128
- int-blasting approaches are identical
- bit-width independent

Term Rewriting  
and All That

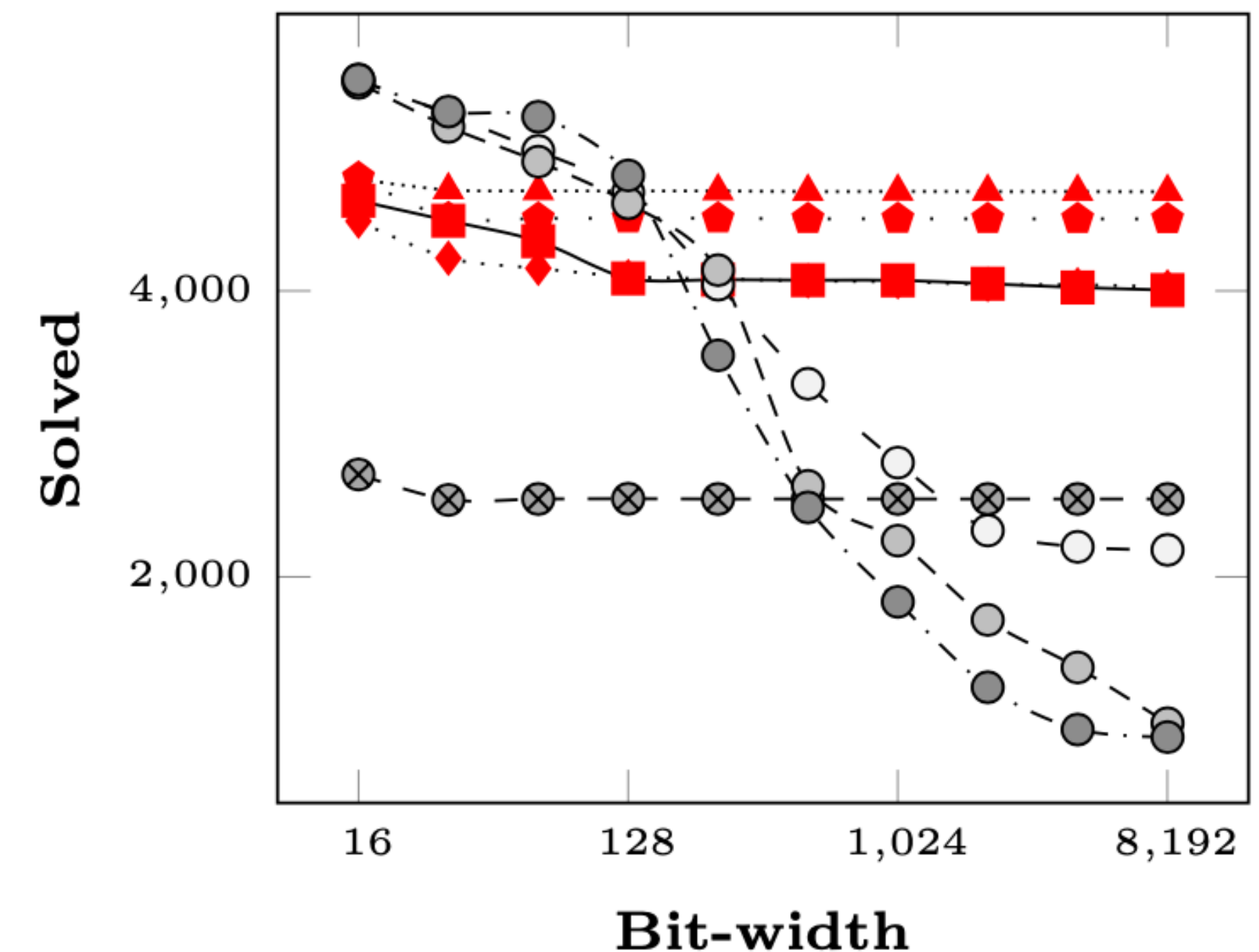


# Results — Rewrite Rules

## Full Set



- Full set: best starting from bit-width 256
- int-blasting approaches are similar
- Almost bit-width independent



Term Rewriting  
and All That

# Smart Contracts Verification

- 35 benchmarks
- Given to us by Certora team
- QF\_UFBV benchmarks with 256-bit bit-vectors
- Employ arithmetic and bitwise operators
- Encode algebraic properties (e.g., commutativity) of low-level methods



# Results – Certora

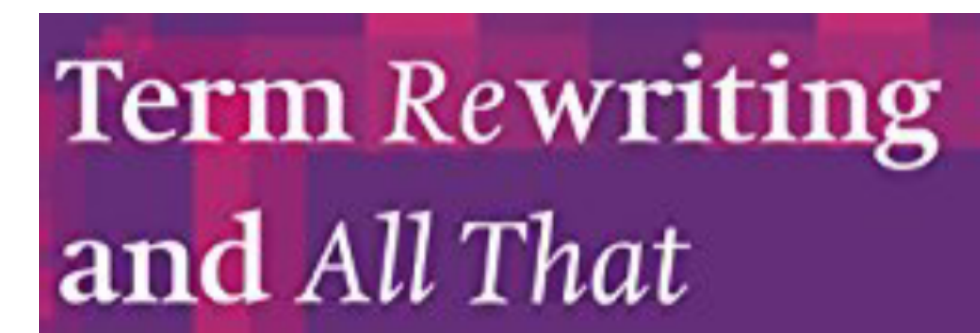
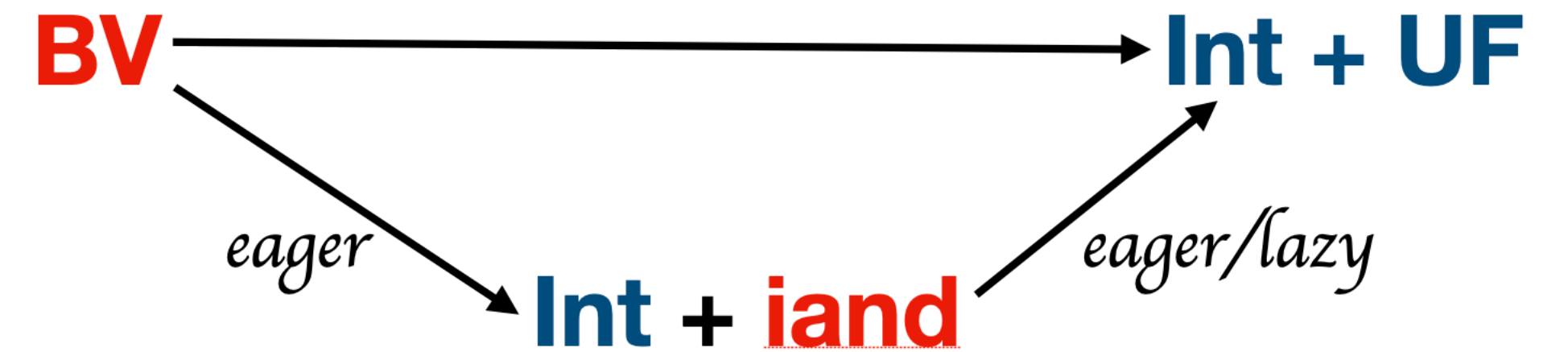
- Timeout: 1 hour
- Int-blasting solved the most
- Int-blasting was faster:
  - 24 benchmarks in 232 seconds
  - 22 benchmarks in 20 seconds
  - Bitwuzla: 16 benchmarks in 5900 seconds
  - Yices: 9 benchmarks in 3900 seconds

	SMT-LIB				ECRW				SC			
	<i>slvd</i>	<i>sat</i>	<i>uns</i>	<i>m</i>	<i>slvd</i>	<i>sat</i>	<i>uns</i>	<i>m</i>	<i>slvd</i>	<i>sat</i>	<i>uns</i>	<i>m</i>
<i>eager<sub>b</sub></i>	35031	10447	24584	38	41989	119	41870	0	<b>24</b>	9	15	0
<i>eager<sub>s</sub></i>	35035	10459	24576	28	41435	119	41316	77	<b>24</b>	9	15	0
<i>lazy<sub>b</sub></i>	35001	10383	24618	23	<b>47071</b>	119	46952	0	<b>24</b>	9	15	0
<i>lazy<sub>s</sub></i>	34819	10297	24522	27	45350	119	45231	138	<b>24</b>	9	15	0
<i>Bitwuzla</i>	41220	14233	26987	19	37297	265	37032	11120	16	8	8	0
<i>cvc5</i>	40543	14204	26339	36	33187	220	32967	17535	-	-	-	-
<i>Yices</i>	<b>41228</b>	14280	26948	11	31646	255	31391	15801	9	3	6	0
<i>bw-ind</i>	-	-	-	-	25608	0	25608	0	-	-	-	-



# Conclusion

- We have seen:
  - Int-blasting is a complement to bit-blasting
  - 4 Configurations (eager/lazy, sum/bitwise)
  - Useful for large bit-widths
- Future Work:
  - Abstraction of other operations (e.g., shift)
  - More benchmarks
  - Improve non-linear integer solver



Thank You!

# What didn't work?

- Granularities: split bit-vectors to blocks of 2s / 4s etc. instead of 1.
  - Sometimes helped, sometimes did not
  - Not explainable, not predictable
- Synthesize lemmas using SyGuS
  - Cumbersome
  - Helped very little
  - smtlib2cvc4



# Results

	SMT-LIB				ECRW				SC			
	<i>slvd</i>	<i>sat</i>	<i>uns</i>	<i>m</i>	<i>slvd</i>	<i>sat</i>	<i>uns</i>	<i>m</i>	<i>slvd</i>	<i>sat</i>	<i>uns</i>	<i>m</i>
<i>eager<sub>b</sub></i>	35031	10447	24584	38	41989	119	41870	0	<b>24</b>	9	15	0
<i>eager<sub>s</sub></i>	35035	10459	24576	28	41435	119	41316	77	<b>24</b>	9	15	0
<i>lazy<sub>b</sub></i>	35001	10383	24618	23	<b>47071</b>	119	46952	0	<b>24</b>	9	15	0
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<i>Bitwuzla</i>	41220	14233	26987	19	37297	265	37032	11120	16	8	8	0
<i>cvc5</i>	40543	14204	26339	36	33187	220	32967	17535	-	-	-	-
<i>Yices</i>	<b>41228</b>	14280	26948	11	31646	255	31391	15801	9	3	6	0
<i>bw-ind</i>	-	-	-	-	25608	0	25608	0	-	-	-	-