

# **CS 498 Expressive Grammars for Natural Language Processing: Theory and Applications**

## **Lecture 15**

Julia Hockenmaier  
juliahr@cs.uiuc.edu

# Where we are

- **Formalisms we have covered so far:**  
Context-free grammars,  
Dependency Grammars,  
Tree-Adjoining Grammars
- **Today: Combinatory Categorical Grammar (CCG)**  
Categories, derivations, non-local dependencies
- **The next lectures:**  
Extracting CCGs from treebanks, building a CCG parser,  
showing the (weak) equivalence of TAG and CCG

# Why categorial grammar?

- Phrase-structure grammar stipulates arbitrary categories and rules.
- Can we define a **calculus over syntactic categories** that
  - does not rely on arbitrary categories or rewrite rules?
  - describes how the meaning of sentences is built compositionally from the meaning of words?

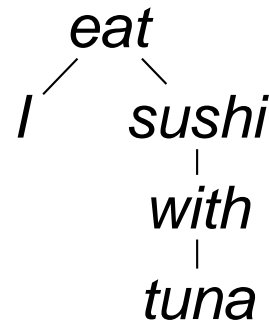
# Why CCG?

- **CCG is mildly context-sensitive** (like TAG)  
Captures crossing dependencies, but is still efficiently parseable
- **CCG has a flexible constituent structure:**
  - Simple, unified treatment of extraction and coordination
  - Psycholinguistic motivation: allows incremental processing
- **CCG has a transparent syntax-semantics interface**  
If we know the syntax of a sentence, we also know its meaning.
- **CCG requires no traces or null elements**  
Parsing algorithms (e.g. CKY) are straightforward to apply.

# What is 'the meaning' of a sentence?

**I eat sushi with tuna**

- A dependency structure:



- A logical formula:

$eat(x, y) \wedge I(x) \wedge sushi(y) \wedge with(y, z) \wedge tuna(z)$

# Overview

- **Part I: The basics**  
**(local dependencies)**
  - The ingredients: categories, rules, derivations
  - Simple syntactic phenomena: modification, simple coordination
  - Syntactic derivations and semantic interpretations
- **Part II: The interesting stuff**  
**(long-range dependencies)**
  - Bounded dependencies: control and raising
  - Unbounded dependencies: extraction and coordination
  - Scrambling

# **Part I: The basics**

# CCG: The machinery

- **Categories** specify subcat lists of words/constituents.
- **Combinatory rules** specify how constituents can combine.
- **The lexicon** specifies which categories a word can have.
- **Derivations** spell out process of combining constituents.



# CCG categories

- Simple categories: **NP**, **S**, **PP**.
- Complex categories: **S\NP**, **(S\NP)/NP**, **(NP\NP)/NP**  
Functions which return a **result** if they get an **argument**:

<b>NP</b>	<b>S\NP</b>	$\Rightarrow$	<b>S</b>
He	drinks coffee		He drinks coffee

<b>(S\NP)/NP</b>	<b>NP</b>	$\Rightarrow$	<b>S\NP</b>
drinks	coffee		drinks coffee

<b>(NP\NP)/NP</b>	<b>NP</b>	$\Rightarrow$	<b>NP\NP</b>
with	milk		with milk

# CCG rules

Function application:

$(S \backslash NP) / NP$   $NP$

$\Rightarrow S \backslash NP$

$NP$   $S \backslash NP$

$\Rightarrow S$

Type raising:

$NP$

$\Rightarrow S / (S \backslash NP)$

Function composition:

$S / (S \backslash NP)$   $(S \backslash NP) / NP$

$\Rightarrow S / NP$

Coordination:

$NP$   $conj$   $NP$

$\Rightarrow NP$

# CCG rules

These are really rule schemas, ie.:

Function application:

$$X/Y \ Y \Rightarrow X$$

$$Y \ X \backslash Y \Rightarrow X$$

Type raising:

$$X \Rightarrow T/(T \backslash X)$$

$$X \Rightarrow T \backslash (T/X)$$

Function composition:

$$X/Y \ Y/Z \Rightarrow X/Z$$

$$Y \backslash Z \ X \backslash Y \Rightarrow X \backslash Z$$

Coordination:

$$X \ \text{conj} \ X \Rightarrow X$$

# CCG rules

These are really rule schemas, ie.:

Function application:

$$X/Y \ Y \Rightarrow X$$

$$Y \ X \backslash Y \Rightarrow X$$

Type raising:

$$X \Rightarrow T/(T \backslash X)$$

$$X \Rightarrow T \backslash (T/X)$$

Function composition:

$$X/Y \ Y/Z \Rightarrow X/Z$$

$$Y \backslash Z \ X \backslash Y \Rightarrow X \backslash Z$$

Coordination:

$$X \ \text{conj} \ X \Rightarrow X$$

These are **order-preserving** rules (context-free only).

More later...

# CCG derivations

$$\frac{\frac{I}{\text{NP}} \quad \frac{\frac{like}{(\text{S} \backslash \text{NP}) / \text{NP}}}{\text{NP}} \quad \frac{coffee}{\text{NP}}}{\text{NP}}$$

# CCG derivations

$$\frac{\frac{I}{\text{NP}} \quad \frac{\text{like}}{(\text{S} \backslash \text{NP}) / \text{NP}} \quad \frac{\text{coffee}}{\text{NP}}}{\text{S} \backslash \text{NP}} >$$

# CCG derivations

$$\begin{array}{c} \frac{I}{\text{NP}} \quad \frac{\text{like}}{(\text{S} \backslash \text{NP}) / \text{NP}} \quad \frac{\text{coffee}}{\text{NP}} \\ \hline \text{S} \backslash \text{NP} \quad > \\ \hline \text{S} \quad < \end{array}$$

# CCG derivations

$$\frac{\frac{I}{\text{NP}} \quad \frac{\frac{\text{like}}{(\text{S} \backslash \text{NP}) / \text{NP}} \quad \frac{\text{coffee}}{\text{NP}}}{\text{NP}}$$



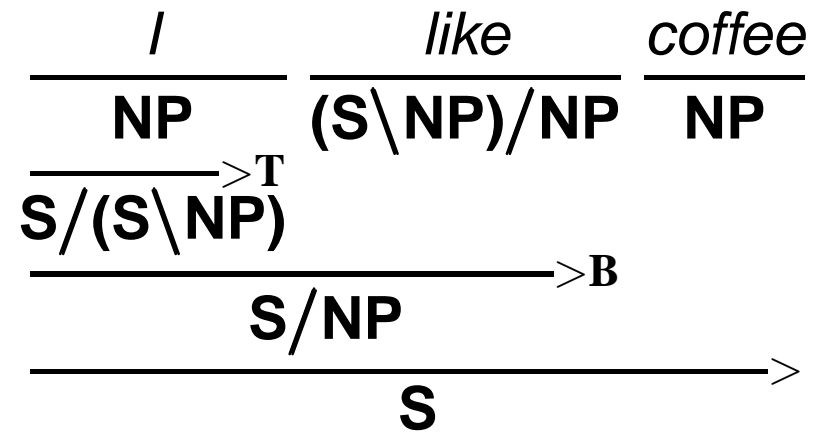
# CCG derivations

$$\frac{\frac{\frac{I}{\text{NP}}}{\text{S}/(\text{S}\backslash\text{NP})}^{>\text{T}} \quad \frac{\frac{like}{(\text{S}\backslash\text{NP})/\text{NP}} \quad \frac{coffee}{\text{NP}}}{\text{S}/(\text{S}\backslash\text{NP})}^{>\text{T}}$$

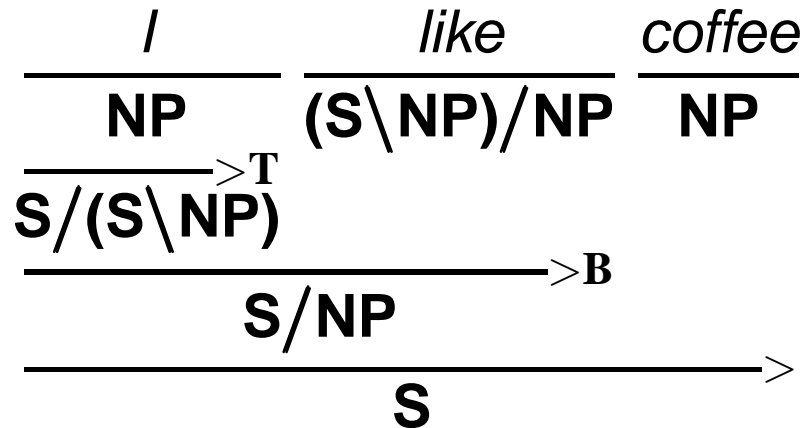
# CCG derivations

$$\begin{array}{c}
 \frac{I}{\text{NP}} \quad \frac{\text{like}}{(\text{S} \backslash \text{NP}) / \text{NP}} \quad \frac{\text{coffee}}{\text{NP}} \\
 \frac{\text{NP}}{\text{S} / (\text{S} \backslash \text{NP})} \xrightarrow{\text{T}} \\
 \frac{\text{S} / (\text{S} \backslash \text{NP})}{\text{S} / \text{NP}} \xrightarrow{\text{B}}
 \end{array}$$

# CCG derivations

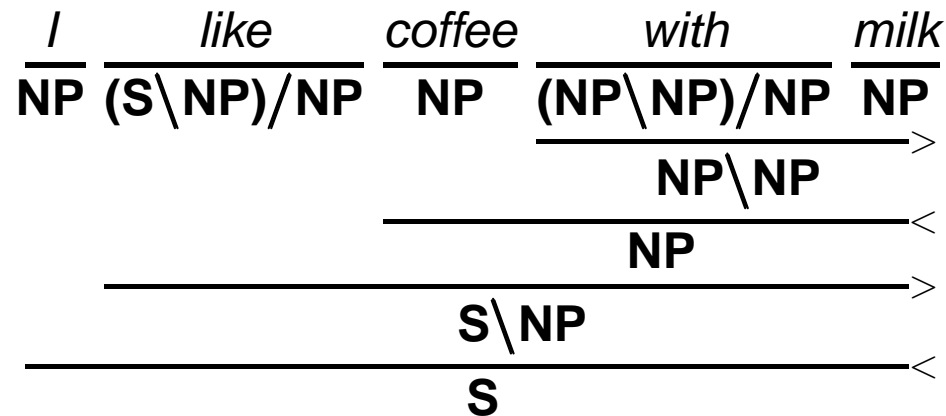


# CCG derivations

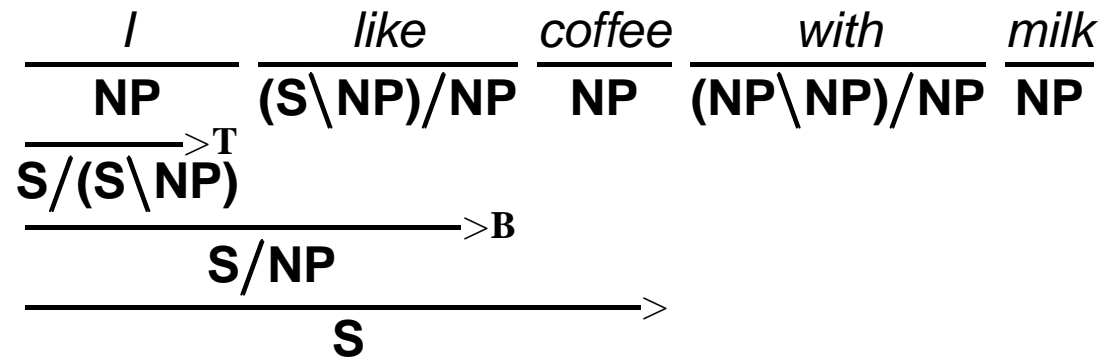


- Type-raising and composition permit alternative derivations.  
This is an example of incremental derivation.
- Here, ***I like*** is a constituent.  
(If you don't like that, we'll later see examples where that makes a lot more sense.)
- But in general, not every substring can be a constituent.

# CCG derivations



but not a fully incremental derivation:



# The syntax-semantics interface

Every syntactic rule has a **semantic interpretation**:

Function application	$\mathbf{X/Y}:\lambda x.f(x) \quad \mathbf{Y}:a$	$\Rightarrow \mathbf{X}:f(a)$
Function composition	$\mathbf{X/Y}:\lambda x.f(x) \quad \mathbf{X/Y}:\lambda x.g(x)$	$\Rightarrow \mathbf{X/Z}:\lambda x.f(gx)$
Type-raising	$\mathbf{X}:a$	$\Rightarrow \mathbf{T/(T \setminus X)}:\lambda f.f(a)$

$$\begin{array}{c}
 \frac{}{\mathbf{NP:I'}} \quad \frac{\frac{\frac{}{\mathbf{like}}}{\mathbf{(S \setminus NP)/NP:\lambda x.\lambda y.like'xy}}}{\mathbf{NP:coffee'}}}{\mathbf{S \setminus NP:\lambda y.like'coffee'y}} > \\
 \hline
 \mathbf{S:like'coffee'I'} <
 \end{array}$$

# The CCG lexicon

- This requires a **lexicon** which pairs words with their syntactic categories and semantic interpretations, e.g:  
**eat**:  $(S \backslash NP) / NP$ :  $\lambda x. \lambda y. eat'(x, y)$ ,  $S \backslash NP$ :  $\lambda x. eat'(x)$   
**sushi**:  $NP$ : *sushi'*  
...
  - CCG is a **lexicalized** formalism:  
The lexicon is where all the language-specific information is represented.

# Approximating predicate-argument structure with word-word dependencies

- The **argument slots** of functor categories define dependencies:

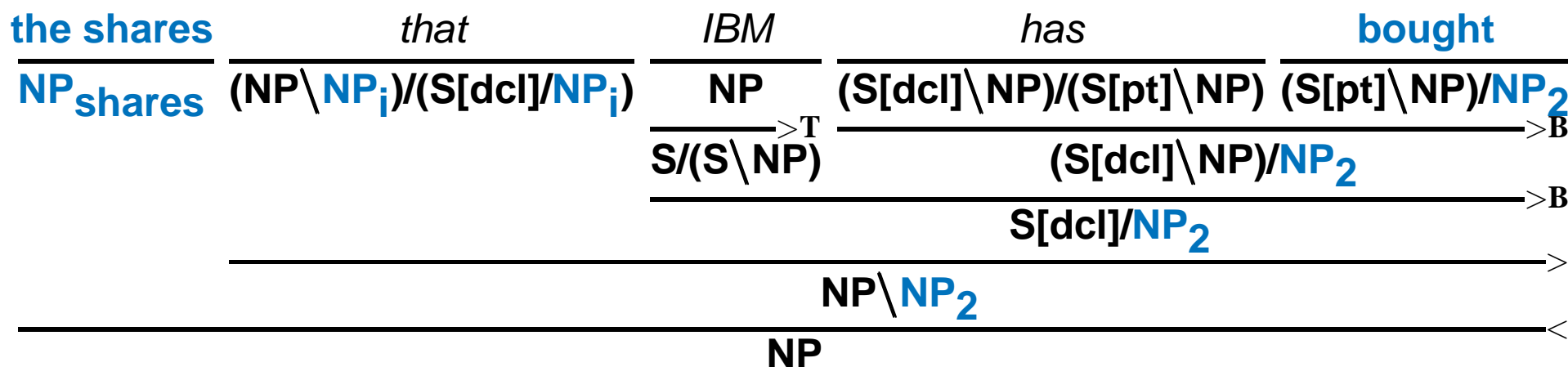
$$\frac{\frac{\textit{like}}{(S[dcl] \backslash NP_1) / NP_2} \quad \frac{\textit{coffee}}{NP}}{S[dcl] \backslash NP_1} >$$

$$\langle \textit{like}, (S[dcl] \backslash NP_1) / NP_2, 2, \textit{coffee} \rangle$$

- This also includes **long-range dependencies**.



# Long-range dependencies in CCG



$\langle \textit{bought}, (S[pt] \backslash NP_1) / NP_2, 2, \textit{shares} \rangle$

- Long-range dependencies are **local**.
- They are **projected from the lexicon** by the derivation.

# Derivations and interpretations

- **Syntactic derivations...**

- ... describe **constituency**
- ... account for **unbounded dependencies**  
that arise through extraction and coordination  
(but don't require traces to do so)
- ... are **not a level of representation** in the theory,  
just a record of the process which builds the interpretation  
(the interface between spoken form and its meaning)

- **Semantic interpretations...**

- ... account for **bounded dependencies**  
that arise in binding, raising and control  
(c-command is defined here)

## **Part II: The interesting parts**

## **A. Bounded dependencies**

# Control and raising

- Bounded dependencies:  
co-index arguments within the lexical category of the verb  
(and re-use the corresponding variable in the semantic interpretation)

*tries*       $((S[dcl] \backslash NP_i) / (S[to] \backslash NP_i)):$        $\lambda p. \lambda y. try'(p(ana'y) y)$   
*persuades*  $((S[dcl] \backslash NP) / (S[to] \backslash NP_i)) / NP_i:$        $\lambda x. \lambda p. \lambda y. persuade'(p(ana'x) x y)$

- Modals and auxiliaries are like subject control:

*might*       $((S[dcl] \backslash NP_i) / (S[b] \backslash NP_i)):$        $\lambda p. \lambda y. might'(p(ana'y) y)$

## **B. Unbounded dependencies**

# Wh-extraction

- Use type-raising and composition to form “incomplete” constituents.
- Wh-words subcategorize for “incomplete” constituents  
(and use co-indexation to pass the dependencies)

# Wh-extraction

- Use type-raising and composition to form “incomplete” constituents.
- Wh-words subcategorize for “incomplete” constituents  
(and use co-indexation to pass the dependencies)

<i>that</i>	<i>John</i>	<i>buys</i>
$(N \setminus N_i) / (S[dcl] / NP_i)$	$NP$	$(S[dcl] \setminus NP) / NP$



# Wh-extraction

- Use type-raising and composition to form “incomplete” constituents.
- Wh-words subcategorize for “incomplete” constituents  
(and use co-indexation to pass the dependencies)

$$\begin{array}{ccc}
 \textit{that} & \textit{John} & \textit{buys} \\
 \hline
 (N \setminus N_i) / (S[dcl] / NP_i) & \text{NP} & (S[dcl] \setminus NP) / NP \\
 & \hline
 & S / (S \setminus NP)^{>T}
 \end{array}$$

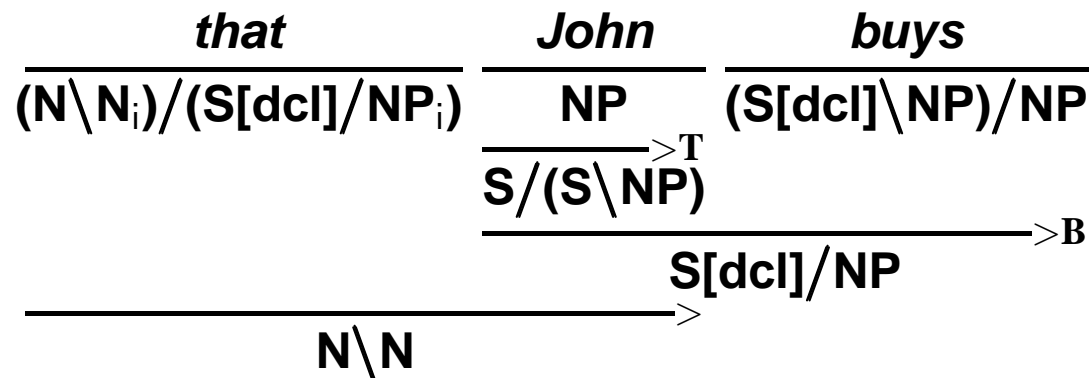
# Wh-extraction

- Use type-raising and composition to form “incomplete” constituents.
- Wh-words subcategorize for “incomplete” constituents (and use co-indexation to pass the dependencies)

$$\begin{array}{c}
 \textit{that} \\
 \hline
 (N \setminus N_i) / (S[\text{dcl}] / NP_i)
 \end{array}
 \quad
 \begin{array}{c}
 \textit{John} \\
 \hline
 NP \\
 \hline
 S / (S \setminus NP)^{>T} \\
 \hline
 S[\text{dcl}] / NP^{>B}
 \end{array}
 \quad
 \begin{array}{c}
 \textit{buys} \\
 \hline
 (S[\text{dcl}] \setminus NP) / NP
 \end{array}$$

# Wh-extraction

- Use type-raising and composition to form “incomplete” constituents.
- Wh-words subcategorize for “incomplete” constituents (and use co-indexation to pass the dependencies)



# Questions

<i>Does</i>	<i>he</i>	<i>seem</i>	<i>to</i>	<i>like</i>	<i>coffee?</i>
$\frac{(S[q]/(S[b]\backslash NP_i))/NP_i}{(S[q]/(S[b]\backslash NP_i))/NP_i}$	$\frac{NP}{NP}$	$\frac{(S[b]\backslash NP)/(S[to]\backslash NP)}{(S[b]\backslash NP)/(S[to]\backslash NP)}$	$\frac{(S[to]\backslash NP)/(S[b]\backslash NP)}{(S[to]\backslash NP)/(S[b]\backslash NP)}$	$\frac{(S[b]\backslash NP)/NP}{(S[b]\backslash NP)/NP}$	$\frac{NP}{NP}$

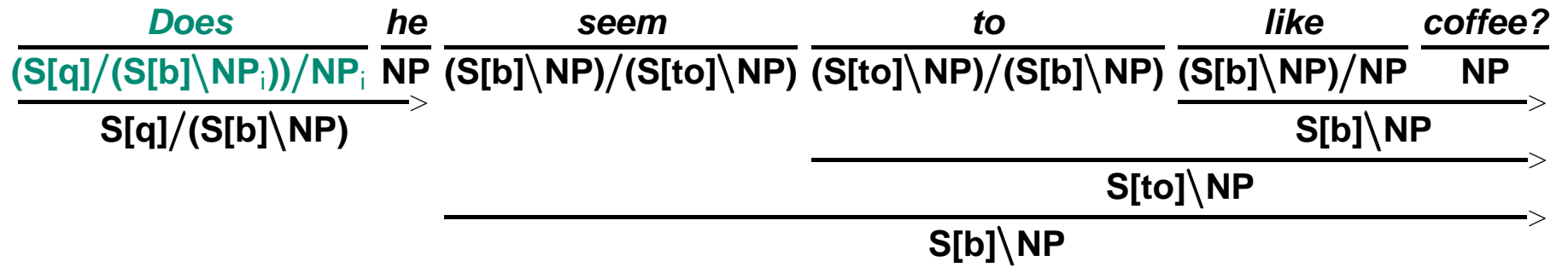
# Questions

<i>Does</i>	<i>he</i>	<i>seem</i>	<i>to</i>	<i>like</i>	<i>coffee?</i>
$\frac{(S[q]/(S[b]\backslash NP_i))/NP_i}{S[q]/(S[b]\backslash NP)} >$	$\frac{NP}{(S[b]\backslash NP)/(S[to]\backslash NP)}$	$\frac{(S[b]\backslash NP)/(S[to]\backslash NP)}{(S[to]\backslash NP)/(S[b]\backslash NP)}$	$\frac{(S[to]\backslash NP)/(S[b]\backslash NP)}{(S[b]\backslash NP)/NP}$	$\frac{(S[b]\backslash NP)/NP}{S[b]\backslash NP} >$	$\frac{NP}{NP}$

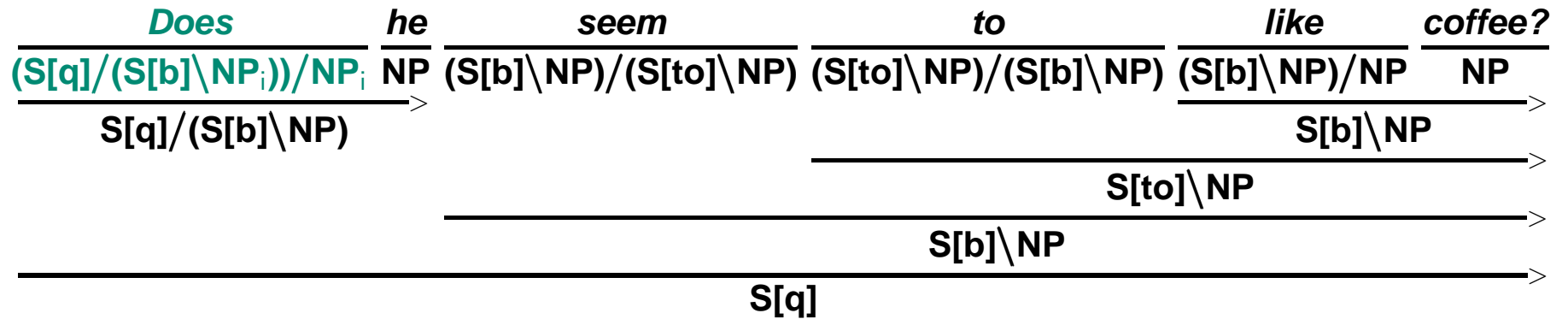
# Questions

<i>Does</i>	<i>he</i>	<i>seem</i>	<i>to</i>	<i>like</i>	<i>coffee?</i>
$\frac{(S[q]/(S[b]\backslash NP_i))/NP_i}{S[q]/(S[b]\backslash NP)}$	$\frac{NP}{S[b]\backslash NP}$	$\frac{(S[b]\backslash NP)/(S[to]\backslash NP)}{(S[to]\backslash NP)/(S[b]\backslash NP)}$	$\frac{(S[to]\backslash NP)/(S[b]\backslash NP)}{(S[b]\backslash NP)/NP}$	$\frac{(S[b]\backslash NP)/NP}{NP}$	$\frac{NP}{NP}$
>				>	
			$S[to]\backslash NP$		>

# Questions

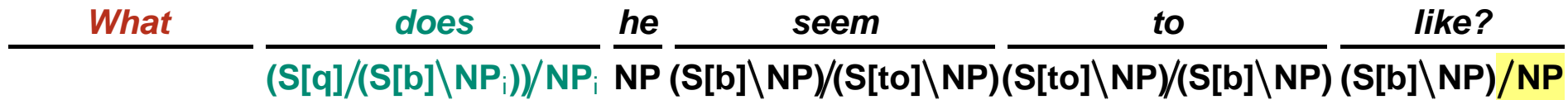
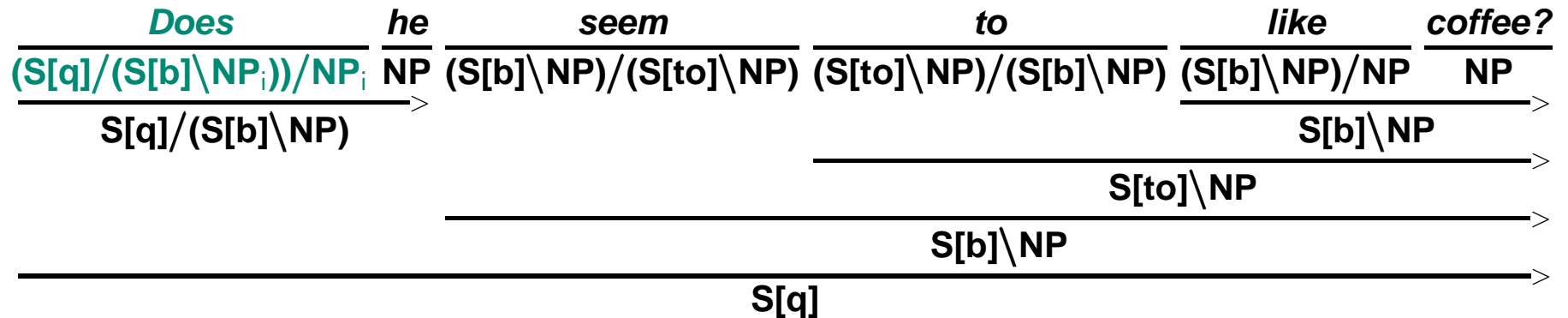


# Questions

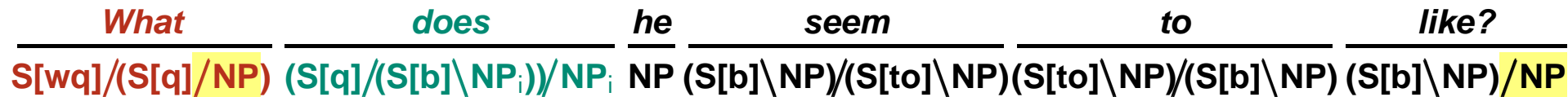
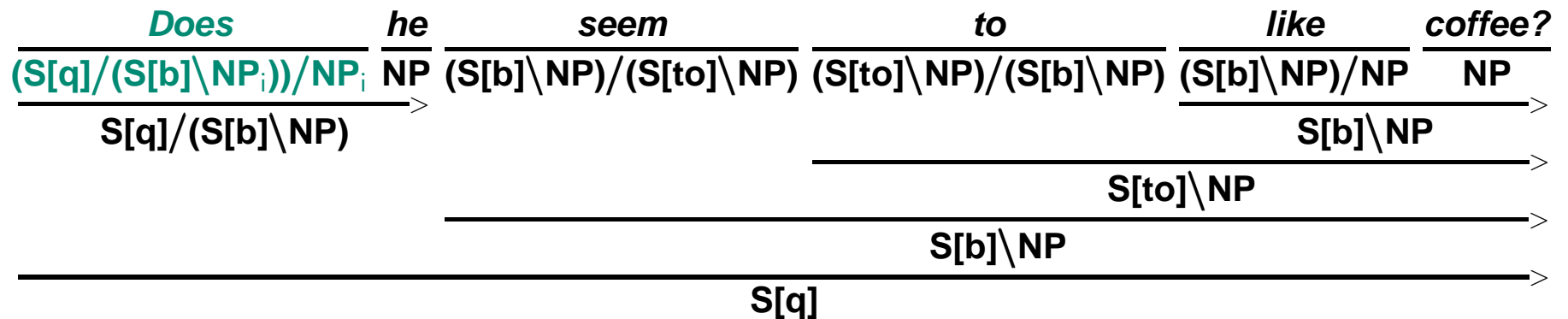




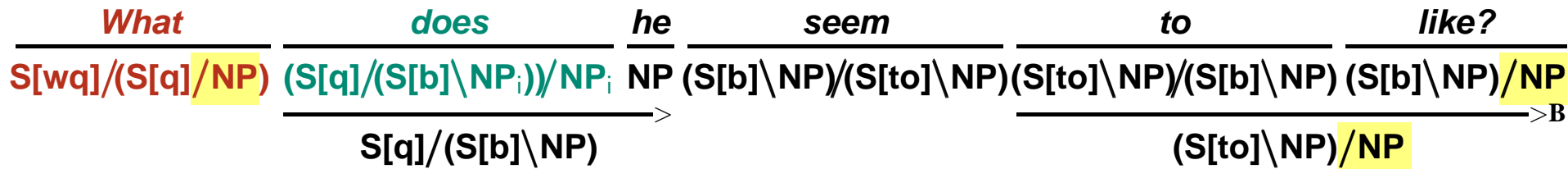
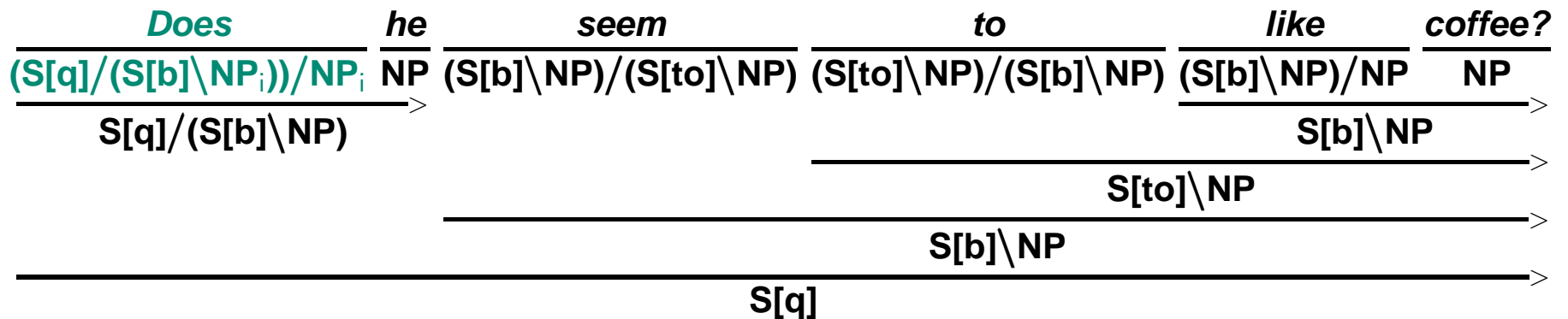
# Questions



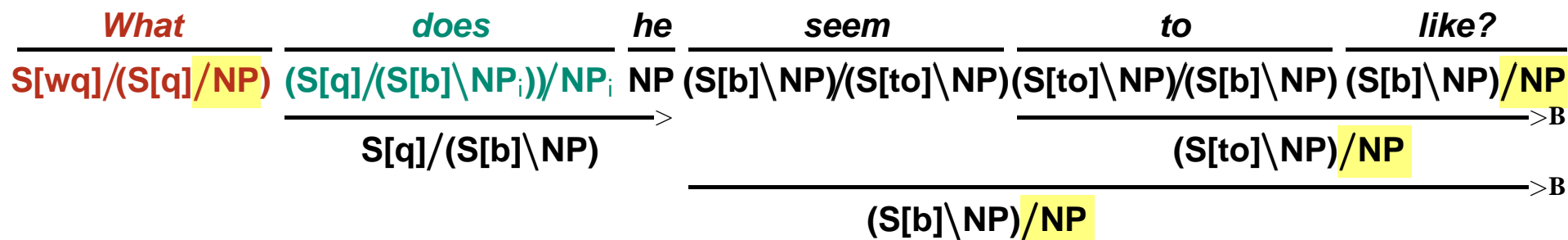
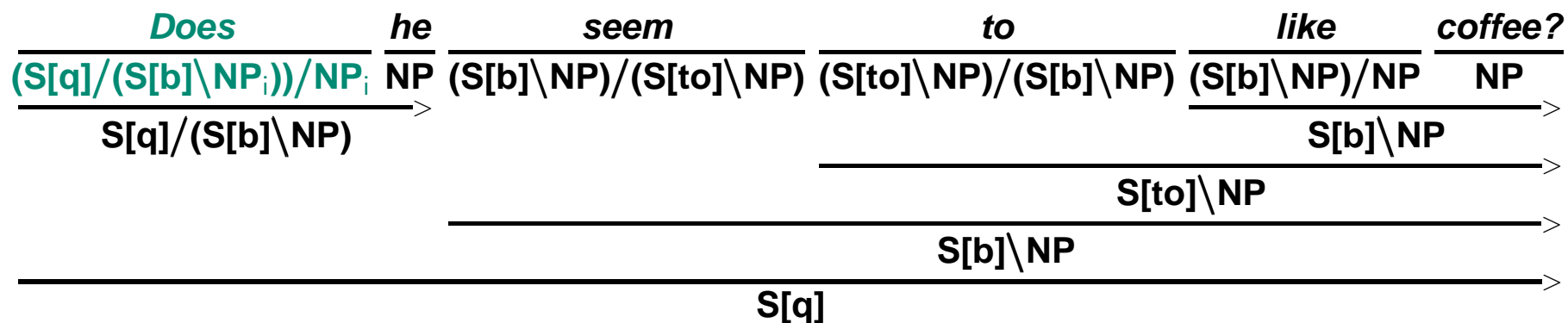
# Questions



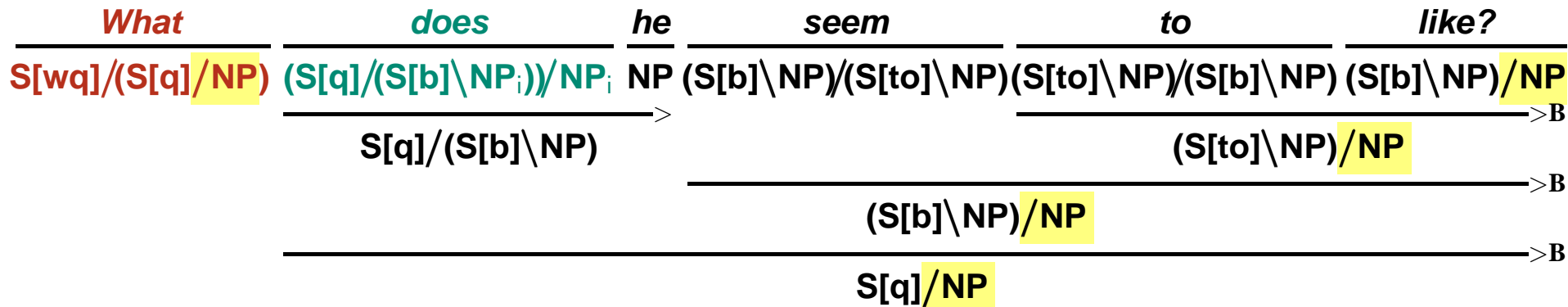
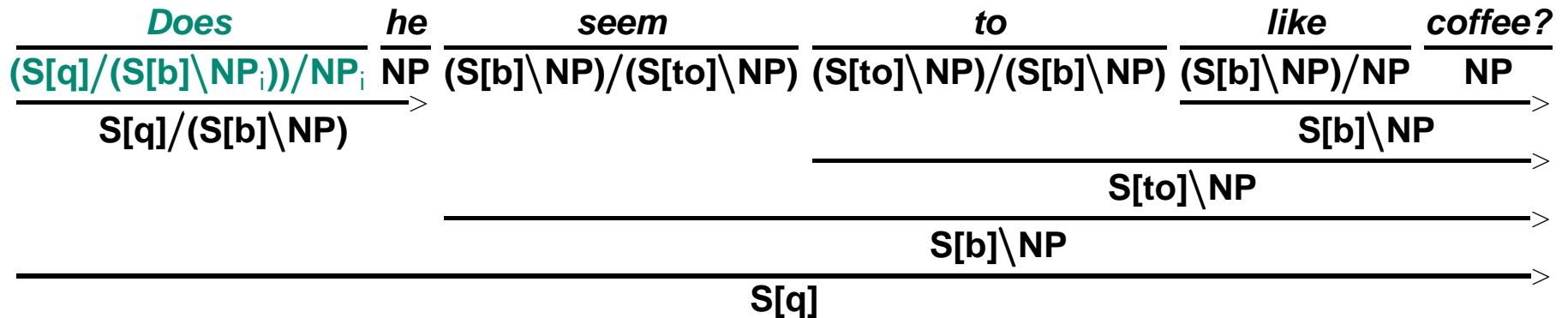
# Questions



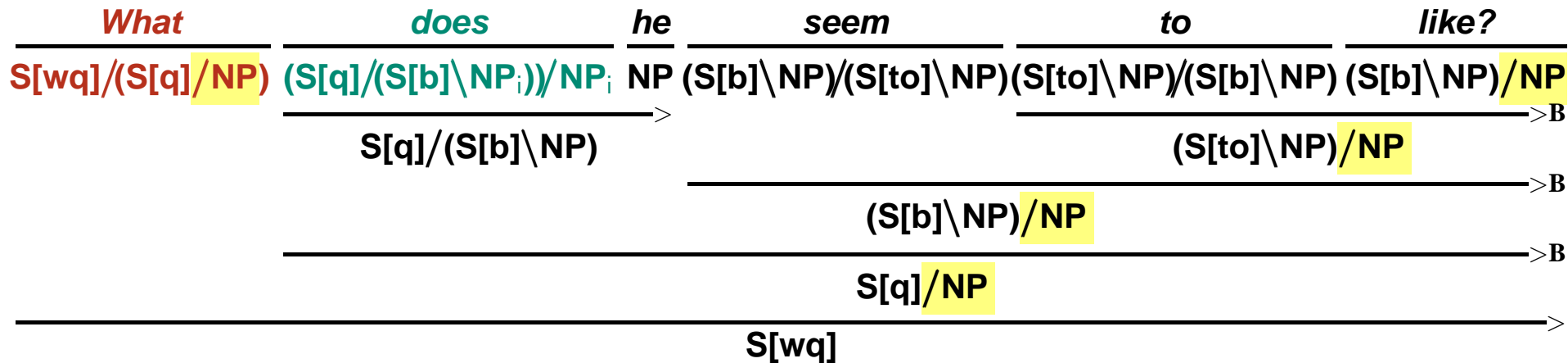
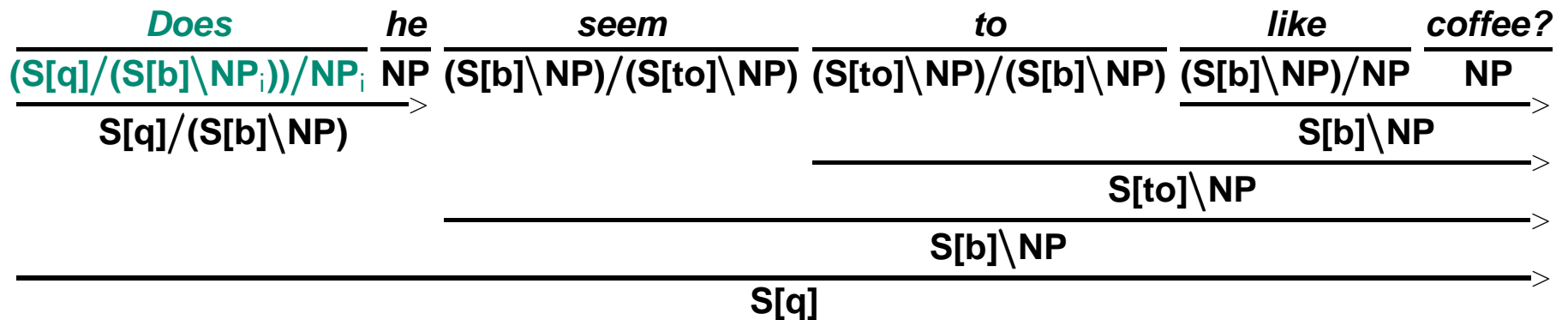
# Questions



# Questions



# Questions



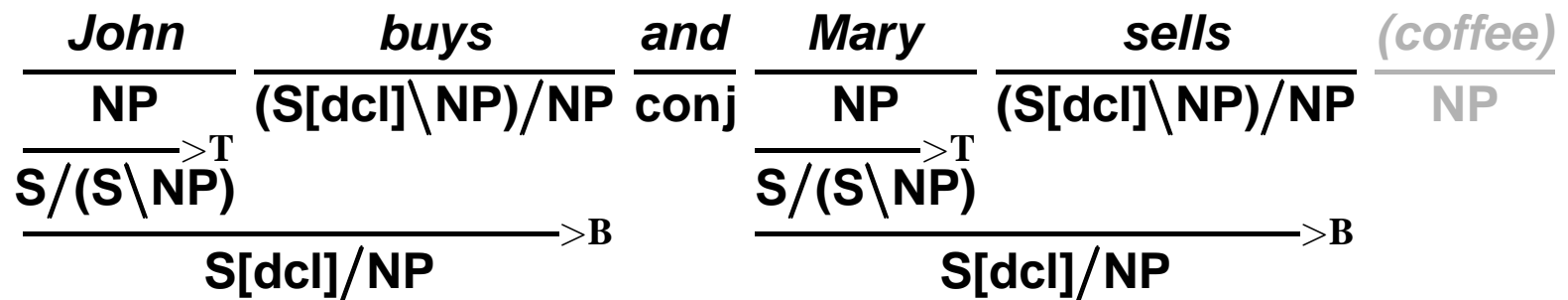
# Right node raising

- Use type-raising and composition to form “incomplete” constituents.
- RNR is just coordination of such “incomplete” constituents:

<i>John</i>	<i>buys</i>	<i>and</i>	<i>Mary</i>	<i>sells</i>	<i>(coffee)</i>
<u>NP</u>	<u>(S[dcl]\NP)/NP</u>	<u>conj</u>	<u>NP</u>	<u>(S[dcl]\NP)/NP</u>	<u>NP</u>

# Right node raising

- Use type-raising and composition to form “incomplete” constituents.
- RNR is just coordination of such “incomplete” constituents:





# Argument cluster coordination

$\frac{I}{\text{NP}}$   $\frac{\text{give}}{((\text{S} \backslash \text{NP}) / \text{NP}) / \text{NP}}$   $\frac{\text{her flowers}}{\text{NP}}$   $\frac{\text{and}}{\text{conj}}$   $\frac{\text{him}}{\text{NP}}$   $\frac{\text{whisky}}{\text{NP}}$

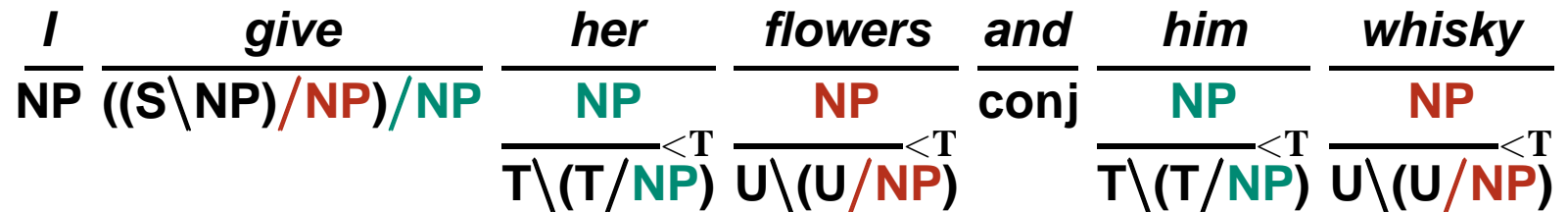
# Argument cluster coordination

- Use type-raising and composition to combine the argument clusters.

<i>I</i>	<i>give</i>	<i>her flowers</i>	<i>and</i>	<i>him</i>	<i>whisky</i>
NP	((S\NP)/NP)/NP	NP	conj	NP	NP

# Argument cluster coordination

- Use type-raising and composition to combine the argument clusters.



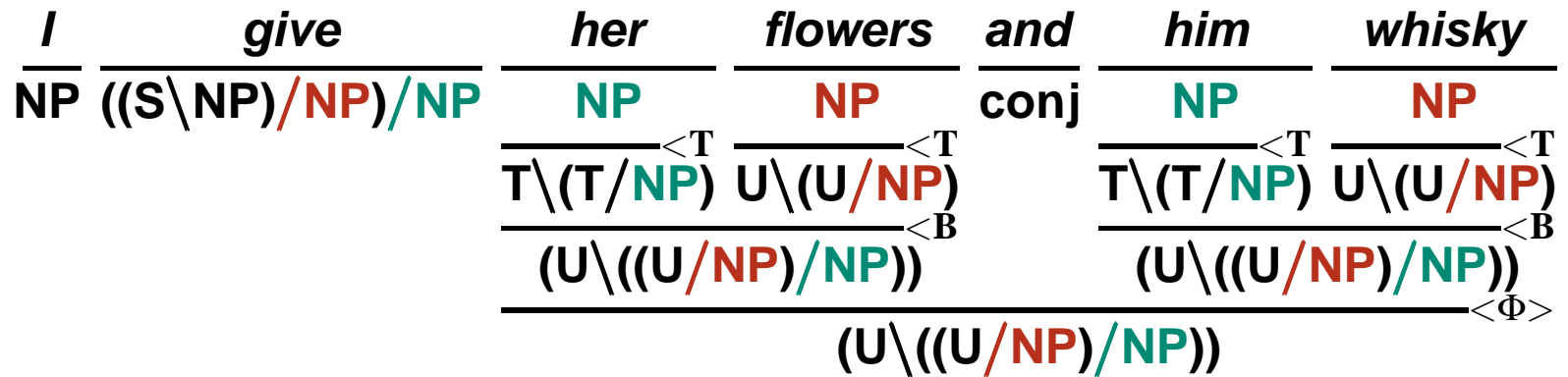
# Argument cluster coordination

- Use type-raising and composition to combine the argument clusters.

$$\begin{array}{c}
 \frac{I}{NP} \quad \frac{give}{((S \backslash NP) / NP)} \quad \frac{her}{NP} \quad \frac{flowers}{NP} \quad \frac{and}{conj} \quad \frac{him}{NP} \quad \frac{whisky}{NP} \\
 \frac{\frac{T \backslash (T / NP)}{U \backslash (U / NP)} \quad \frac{T \backslash (T / NP)}{U \backslash (U / NP)}}{(U \backslash ((U / NP) / NP))} \quad \frac{\frac{T \backslash (T / NP)}{U \backslash (U / NP)} \quad \frac{T \backslash (T / NP)}{U \backslash (U / NP)}}{(U \backslash ((U / NP) / NP))}
 \end{array}$$

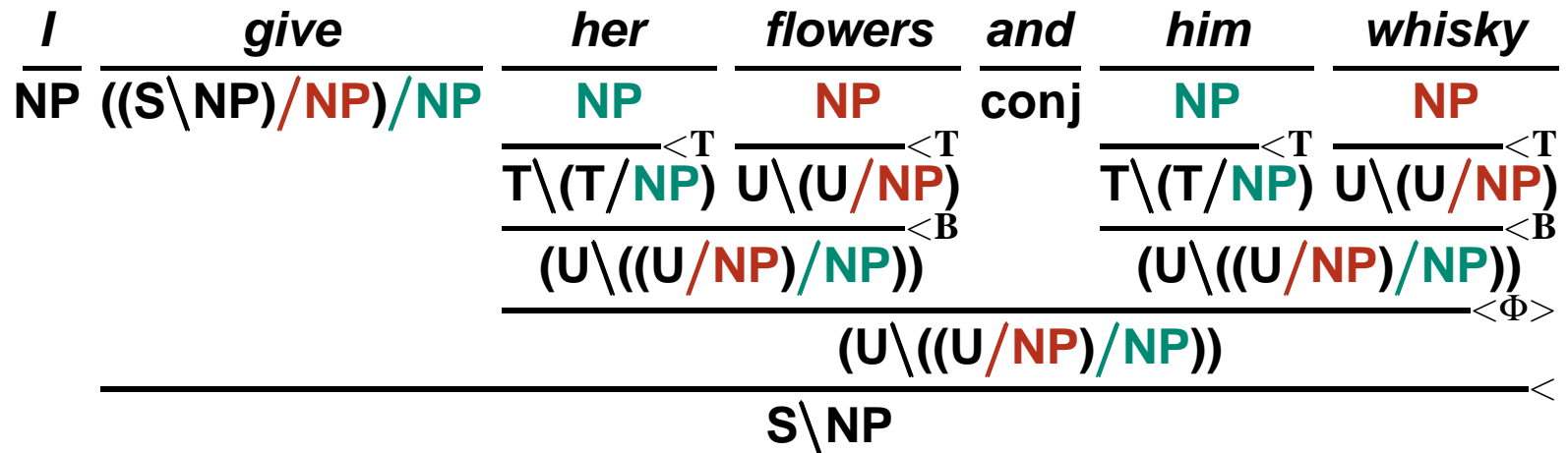
# Argument cluster coordination

- Use type-raising and composition to combine the argument clusters.



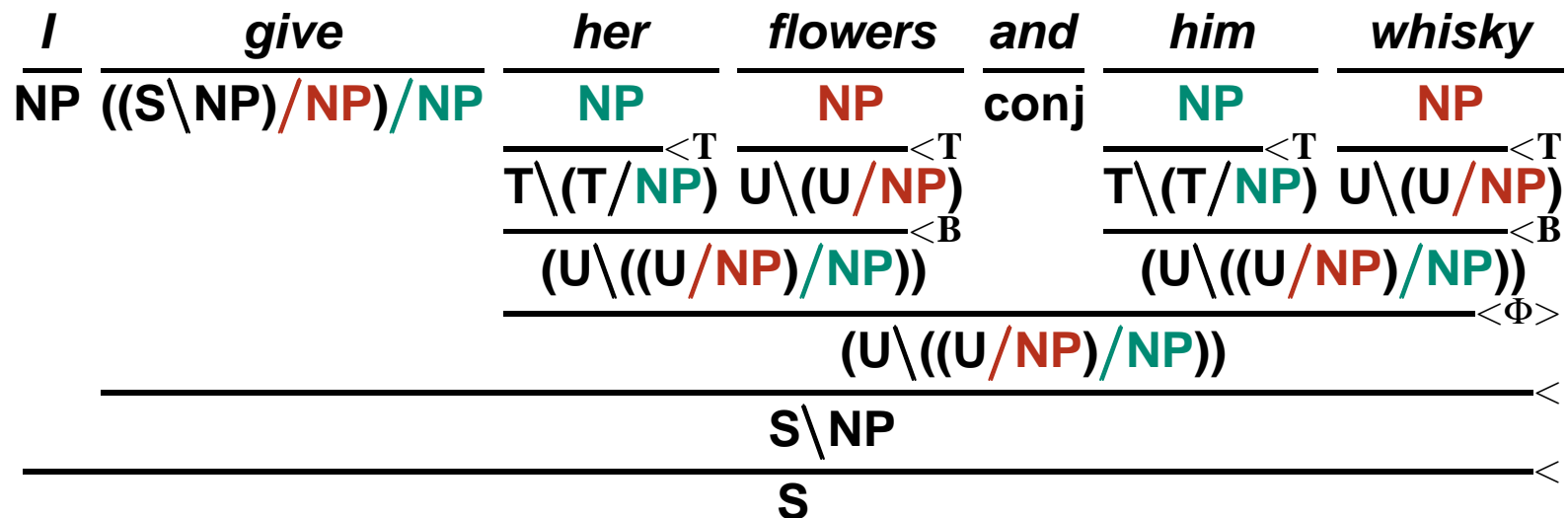
# Argument cluster coordination

- Use type-raising and composition to combine the argument clusters.



# Argument cluster coordination

- Use type-raising and composition to combine the argument clusters.



# Scrambling

Verb has standard category. Use type-raising and (crossing) composition

