# **JPEG Quantization Tables for GPS Maps**

### Yair Wiseman\*

Computer Science Department, Bar-Ilan University, Ramat-Gan, 52900 Israel
\*e-mail: wiseman@cs.biu.ac.il
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**Abstract**—Controlling the quality of the images in JPEG is done by quantization tables. There are two quantization tables — one for the luminance information and one for the chrominance information. These tables have been designed for images with few sharp changes; however, typically most GPS image maps have many sharp changes; therefore, the images are not optimally compressed. In this paper we suggest to revise the standard quantization tables, so they will be more suitable for GPS image map compression.

Keywords: image compression, JPEG, GPS, quantization tables

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## 1. INTRODUCTION

JPEG is a longstanding image compression format. JPEG stands for "Joint Photographic Experts Group," which is the working group name which was established in 1986 by the CCITT and ISO Standards organizations with the intention of generating a standard for image compression. The group completed the design of the standard by early 1991, and, after that, the standard was accepted by the International Standards Organization (ISO) [1].

The first versions of JPEG had only an average compression ratio of 15:1; however, in recent years, JPEG has been succeeding to obtain much better compression ratios. These better compression ratios have been enabling real-time, full-motion, and video applications to employ JPEG [2, 3]. Also the feature of automatic error correction of JPEG promoted the format popularity [4, 5].

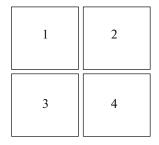
GPS systems [6, 7] usually make use of maps divided into small squares [8]. These small squares are commonly compressed by the JPEG algorithm so as to make the size of the data smaller [9, 10]; however, no distinctive optimization for JPEG quantization tables for images of GPS maps has been proposed to the Joint Photographic Experts Group with the aim of better handling of these maps.

The algorithm of the JPEG compression standard is sketchily explained herein below:

JPEG makes use of the Chroma subsampling method of image encoding. This method supports lower resolution for chrominance data; whereas luminance data have a better resolution. This subsampling method takes advantage of the lower sensitiveness of usual human eyes to chrominance data.

Initially, JPEG converts the original image color into a suitable color space. Usually JPEG converts the image into YUV components [11]. The YUV components are interleaved together within the compressed data; however, the ratio between the Y components, the U components, and the V components will typically not be one to one. The Y components will typically appear four times more than the U components and the V components. The Y components represent the luminance data of the block, whereas the U components and the V components represent the chrominance information of the block. For the reason that usual human eyes are more sensitive to the data of the Y components, more data is stored for the Y components in JPEG compressed file [12]. Specifically, the arrangement of the blocks in a JPEG compressed file is four Y components, one U component, and one V component. Thereafter, repeatedly, four Y components, one U component, and one V component are stored, whereas each component represents the data of  $8\times 8$  pixels block.

This technique of quartered resolution of the U components and the V components is called 4:1:1 chroma subsampling, which denotes that the luminance data and the chrominance data are in quantity of four for the luminance data, one for the U chrominance data, and one for the V chrominance data. Specifically, for each sampled block of  $16 \times 16$  divided to four blocks of  $8 \times 8$  as in Fig. 1, there are four Y



**Fig. 1.** JPEG sampled block of  $16 \times 16$ .

components of luminance and only one U component of chrominance and one V component of chrominance [13].

However, there is another chroma subsampling technique of JPEG which is named 4:2:0. In this subsampling technique, the horizontal sampling of the U components and the V components is doubled compared to 4:1:1 chroma subsampling, but the vertical sampling of the U components and the V components is equal to 4:1:1 chroma subsampling and the U components and the V components are sampled only on each alternate line.

JPEG supports values of 8 bits or 12 bits, which results in a range of 0–255 for 8 bits and 0–4095 for 12 bits. 8 bits are more common in use. These values are modified from unsigned integers in the range of  $[0, 2^p - 1]$  to signed integers in the range of  $[-2^{p-1}, 2^{p-1} - 1]$ , by reducing  $2^{p-1}$  from their original values, where p is the precision (8 or 12) [14]. Next, these modified values are the input of the FDCT function.

JPEG gathers all the  $8 \times 8$  values to one block. The blocks are arranged in lines from left to right from the top line of the image to the bottom line of the image. After that, JPEG converts each block to a frequency space using the forward discrete cosine transform (FDCT) [15]. This conversion keeps lower frequency data which human eyes are more sensitive to [16].

Next, the quantization is performed. For each block, each of its 64 values is divided by a predefined quantization coefficient and rounded to an integer value. Therefore, dividing by a large quantization coefficient will cause more information loss, so the quantization coefficients are decided according to the preferred balance between the compressed file size and the image quality.

The image maker decides about a number from 1 to 100 which denotes the image quality. The value 1 is the poorest image quality and the best compression ratio, whereas the value 100 is the best image quality and the poorest compression ratio. Actually, value 100 denotes a quantization table full of 1s which results in a smaller loss, because there is no loss in the dividing step, only the rounding causes a minor loss.

It is important to note that there is no standard practice for building the quantization table from the selected image quality, so the entire quantization table is stored in the compressed image file.

The last step of JPEG is reducing the file size by a version of canonical Huffman compression [17]. JPEG also supports arithmetic coding [18], but the default is the canonical Huffman compression [19, 20]. Since most of the image makers prefer to use the default, the use of arithmetic code is very limited. Additional compression algorithms have been suggested for JPEG, but the official standard does not specify them as supported algorithms and the most of the conventional applications does not support them [21].

This paper suggests improved quantization tables for JPEG images of GPS maps with the intention of generating a small information size.

## 2. CURRENT QUANTIZATION TABLES

There have been suggestions for improvement of JPEG quantization tables for specific uses [22]. The standard quantization tables are designed for general purpose; however, these tables are not suitable for every application. As a matter of fact, these standard quantization tables appear to be more suitable for images containing no sharp changes in the colors [23]. Images of maps usually contain many sharp changes in the colors. Therefore, assuming that many changes in color do occur, the standard quantization tables can be adjusted with the purpose of producing better compression ratio.

The standard quantization tables of 90%, which are commonly used in GPSes, are presented in Figs. 2a and 2b.

| (a) |    |    |    |    |    |    |    |  |
|-----|----|----|----|----|----|----|----|--|
| 3   | 2  | 2  | 3  | 5  | 8  | 10 | 12 |  |
| 2   | 2  | 3  | 4  | 5  | 12 | 12 | 11 |  |
| 3   | 3  | 3  | 5  | 8  | 11 | 14 | 11 |  |
| 3   | 3  | 4  | 6  | 10 | 17 | 16 | 12 |  |
| 4   | 4  | 7  | 11 | 14 | 22 | 21 | 15 |  |
| 5   | 7  | 11 | 13 | 16 | 21 | 23 | 18 |  |
| 10  | 13 | 16 | 17 | 21 | 24 | 24 | 20 |  |
| 14  | 18 | 19 | 20 | 22 | 20 | 21 | 20 |  |
|     |    |    |    |    |    |    |    |  |
| (b) |    |    |    |    |    |    |    |  |
| 3   | 4  | 5  | 9  | 20 | 20 | 20 | 20 |  |

| 3  | 4  | 5  | 9  | 20 | 20 | 20 | 20 |
|----|----|----|----|----|----|----|----|
| 4  | 4  | 5  | 13 | 20 | 20 | 20 | 20 |
| 5  | 5  | 11 | 20 | 20 | 20 | 20 | 20 |
| 9  | 13 | 20 | 20 | 20 | 20 | 20 | 20 |
| 20 | 20 | 20 | 20 | 20 | 20 | 20 | 20 |
| 20 | 20 | 20 | 20 | 20 | 20 | 20 | 20 |
| 20 | 20 | 20 | 20 | 20 | 20 | 20 | 20 |
| 20 | 20 | 20 | 20 | 20 | 20 | 20 | 20 |

Fig. 2. (a) JPEG luminance quantization table of 90% and (b) JPEG chrominance quantization table of 90%.

The designers of these quantization tables have assumed that the chances for sharp changes in the colors are quite slight. Therefore, they put larger numbers in the right lower part of the quantization tables, so, when the values in the right lower part of the block will be divided by these numbers, a significant amount of data will be gone. If indeed not much data are stored in the right lower part of the blocks, such quantization tables can be very effective. However, in blocks of images with sharp changes in the colors, the difference between the left upper part and the lower right part of the quantization tables will be smaller.

In the standard quantization tables of 90%, the difference between the highest value and the smallest value is about 7 times. In standard quantization tables of less than 90% the difference becomes even more substantial and can be easily even more than 10 times. When there are sharp changes in the pictures, these differences are not suitable and must be reduced.

The sharp changes in the images of maps do not have an effect only on the AC values in the blocks, but also on the DC values. The most upper left value of each  $8 \times 8$  block is called DC [24]. DC is the sum of the sampling values in the block divided by eight; however, since the algorithm of JPEG presumes that sharp changes in the color do not often occur, the difference between the DCs of adjacent blocks is expected to be small [25], so it is better to store the difference between the previous DC value and the current DC value which is anticipated to be smaller than the DC value itself and therefore can be compressed better [19, 20].

In images of GPS maps, sharp changes are more likely to occur, so the DC differences might be higher and even if a DC difference is divided by a larger number, it will not be zeroing.

## 3. ADJUSTED QUANTIZATION TABLES FOR GPS MAPS

There have been several works about identifying sharp changes in JPEG images, so as to utilize these sharp changes for a number of applications such as detection of a cancerous lesion [26, 27], finding damages in tires [28–30], locating damages in fuselages [33, 34], observing of traffic congestions [33–35], an alert system for worn out pipes in autonomous vehicles [36], safety mechanism for SkyTran tracks [37], and adjustable flush toilet [38].

We suggest adjusting the quantization tables for images with sharp changes. The sharp changes in the colors give rise to a smaller difference between the left upper part and the lower right part of the JPEG blocks. Therefore, an adjustment of the quantization tables can provide a better compression ratio.

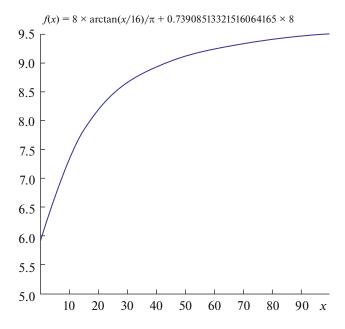


Fig. 3. Graph of the luminance quantization table values.

Usually, there is still difference between the left upper part and the lower right part of the JPEG blocks of GPS maps, but the difference is smaller, so we suggest for the luminance component formula (1):

$$f(x) = \frac{8 \tan^{-1} \left(\frac{x}{16}\right)}{\pi} + 8DOTTIE,$$
(1)

where  $x = X^2 + Y^2$ , X is the index of the coefficient in the X-axis, Y is the index of the coefficient in the Y-axis, f(x) is the value of the coefficient in the quantization table, and *DOTTIE* is the Dottie number [39]. The graph of the formula is depicted in Fig. 3.

For the chrominance quantization table we suggest formula (2):

$$f(x) = \pi \tan^{-1} \left(\frac{x}{16}\right) + 8DOTTIE,\tag{2}$$

where  $x = X^2 + Y^2$ , X is the index of the coefficient in the X-axis, Y is the index of the coefficient in the Y-axis, f(x) is the value of the coefficient in the quantization table, and *DOTTIE* is the Dottie number.

The graph of the formula is depicted in Fig. 4.

Accordingly, the new quantization tables are shown in Figs. 5a and 5b.

In both of the luminance quantization table and the chrominance quantization table the values of the lower right part have been reduced and the values of upper left part have been increased in order to make smaller differences between the coefficients produced by the DCT algorithm.

## 4. EXPERIMENTAL RESULTS

Figure 6a contains an image of a GPS map [40] of a region in Jerusalem, Israel, compressed by JPEG with standard quantization tables. The image contains many sharp changes. Therefore, the standard quantization tables are not so suitable for a proper compression.

Figure 6b contains the same image, but compressed with the suggested adjusted quantization tables. The differences between the images are unnoticeable; however, the standard quantization tables produced a file size of 130991 B, whereas the suggested adjusted quantization tables produced a file size of 120303 B. That is to say a save of 8.16%.

It should be noted that sometimes images of GPS maps can be with almost no sharp changes like a road in an uninhabited region. Figure 7a contains an image of a GPS map of an uninhabited region in the Negev district, Israel. This image has been compressed using the standard quantization tables.

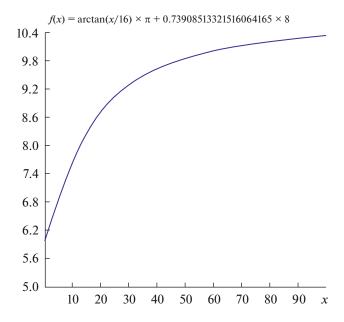


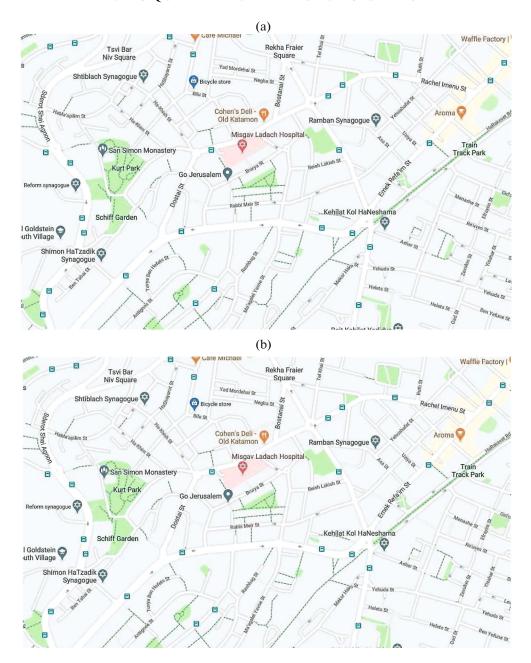
Fig. 4. Graph of the chrominance quantization table values.

| (a) |     |    |    |    |    |    |    |  |  |  |
|-----|-----|----|----|----|----|----|----|--|--|--|
| 6   | 6   | 6  | 6  | 8  | 8  | 9  | 9  |  |  |  |
| 6   | 6   | 6  | 6  | 8  | 8  | 9  | 9  |  |  |  |
| 6   | 6   | 6  | 6  | 8  | 8  | 9  | 9  |  |  |  |
| 6   | 6   | 6  | 8  | 8  | 9  | 9  | 9  |  |  |  |
| 8   | 8   | 8  | 8  | 9  | 9  | 9  | 9  |  |  |  |
| 8   | 8   | 8  | 9  | 9  | 9  | 9  | 9  |  |  |  |
| 9   | 9   | 9  | 9  | 9  | 9  | 9  | 9  |  |  |  |
| 9   | 9   | 9  | 9  | 9  | 9  | 9  | 9  |  |  |  |
|     | (b) |    |    |    |    |    |    |  |  |  |
| 6   | 6   | 6  | 6  | 8  | 8  | 9  | 10 |  |  |  |
| 6   | 6   | 6  | 6  | 8  | 8  | 9  | 10 |  |  |  |
| 6   | 6   | 6  | 6  | 8  | 8  | 9  | 10 |  |  |  |
| 6   | 6   | 6  | 8  | 8  | 9  | 9  | 10 |  |  |  |
| 8   | 8   | 8  | 8  | 9  | 9  | 10 | 10 |  |  |  |
| 8   | 8   | 8  | 9  | 9  | 10 | 10 | 10 |  |  |  |
| 9   | 9   | 9  | 9  | 10 | 10 | 10 | 10 |  |  |  |
| 10  | 10  | 10 | 10 | 10 | 10 | 10 | 10 |  |  |  |

Fig. 5. (a) New JPEG luminance quantization table and (b) new JPEG chrominance quantization table.

Figure 7b contains the same image as Fig. 7a; however, In Fig. 7b the image has been compressed by the suggested adjusted quantization tables. The sizes of the images are exactly the same size of Figs. 6a and 6b; however, because there are very few sharp changes in Figs. 7a and b, the images' size is smaller.

The size of the image in Fig. 7a is 14015 B; whereas the size of Fig. 7b is 14203 B. In other words, the size of the image compressed by the suggested adjusted quantization tables is larger than the size of the image compressed by the standard quantization tables. The addition is not large, only 1.34%, but since the suggested adjusted quantization tables have been designed for images with many sharp changes, there will be a small increase in the file sizes if the image contains very few sharp changes.



**Fig. 6.** (a) GPS map of a region in Jerusalem compressed by the standard quantization tables and (b) GPS map of a region in Jerusalem compressed by the suggested adjusted quantization tables.

It should be noted that there is no change in the clarity of the maps when using the suggested adjusted quantization tables regardless of the image content, i.e., many sharp changes or few sharp changes do not change the quality of the image.

## 5. CONCLUSIONS

GPS stores many map images in its memory [41, 42]. To accommodate these memory needs, compression can be applied [43, 44]. We suggest a technique to obtain a lower compressed file size of GPS image compressed by JPEG algorithm without changing the algorithm itself. We just modify the quantization tables that are stored within the JPEG images. The proper quantization tables for images with many sharp changes are different from quantization tables for images with few sharp changes. The sharp changes in the colors generate a smaller difference between the left upper part and the lower right part of the JPEG

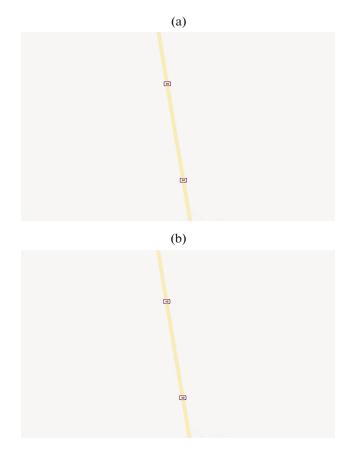


Fig. 7. GPS map of a region in an uninhabited region compressed (a) by the standard quantization tables and (b) by the suggested adjusted quantization tables.

blocks. Therefore, as we have shown in this paper, an adjustment of the JPEG quantization tables can provide a better compression ratio in images containing GPS maps.

## CONFLICT OF INTEREST

The author declares that he has no conflicts of interest.

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