Inductive learning hypothesis: any hypothesis found to approximate the target function well over a sufficiently large set of training examples will also approximate the target function well over any other unobserved examples.

Assumptions for Inductive Learning Algorithms:

- The training sample represents the population
- The input features permit discrimination

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k-nearest neighbor

Also called instance-based Learning; case-based learning. A: set of features/attributes, A_1, \ldots, A_n that describe the problem

 $x = x_{a_1} x_{a_2} \dots x_{a_n}$, where x_{a_i} is the value of feature A_i in example x

$$f(x): x \to c\epsilon C = \{c_1, \dots, c_m\}$$

The case base is the set of training examples $(x_1, f(x_1)), (x_2, f(x_2)), \ldots$

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Inductive Learning

System tries to induce a general rule from a set of observed instances.



The *hypothesis* produced is sometimes called the *concept* description — essentially a program that can be used to classify subsequent instances.

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k-nearest neighbor algorithm for computing f(x):

1. Compare new example, x, to each case, y, in the case base and calculate for each pair:

$$sim(x,y) = \sum_{i=1}^{n} match(x_{a_i}, y_{a_i})$$

where match(a, b) is a function that returns 1 if a and b are equal and 0 otherwise.

- 2. Let R = the top k cases ranked according to sim
- 3. Return as f(x) the class, c, that wins the majority vote among $f(R_1), f(R_2), \ldots, f(R_{|k|})$. Handle ties randomly.

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Types of Attributes

- 1. Symbolic (nominal) $EyeColor \in \{brown, blue, green\}$
- 2. Boolean $anemic \in \{TRUE, FALSE\}$
- 3. Numeric (Integer, Real) $age \in [0, 105]$

How do we compute the similarity between EyeColor = brown and EyeColor = green?

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k-Nearest Neighbor Algorithm

- 1. Memorizes all observed instances and their class
- 2. Is this rote learning?
- 3. Is this really learning?
- 4. When does the induction take place?

Example of case retrieval for k-nn

outlook	temp	humidity	windy	plan	sim
sunny	hot	high	false	cs472	
sunny	hot	high	true	cs472	
overcast	hot	high	false	soccer	
overcast	mild	$_{ m normal}$	true	football	
rain	mild	high	false	soccer	
rain	cool	$_{ m normal}$	false	soccer	

A: outlook, temp, humidity, windy

 $k = 1, C = \{\text{soccer, cs472 football}\}$

 $test\ case:\ X={
m sunny\ cool\ high\ false}$

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Advantages and Disadvantages

What constitutes the concept description?

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